Chapter 2
PHYSICAL AND LINK LAYER
Mobile Computing
Summer 2004
Overview

• Frequencies
• Signals
• Antenna
• Modulation
• Signal propagation

• Multiplexing
• Spread spectrum
• CDMA
Frequencies

VLF  LF  MF  HF  VHF  UHF  SHF  EHF  infrared  visible light  UV

1 Mm  10 km  100 m  1 m  10 mm  100 µm  1 µm
300 Hz  30 kHz  3 MHz  300 MHz  30 GHz  3 THz  300 THz

twisted pair  coax  ISM  AM  SW  FM
## Frequencies and regulations

- ITU-R holds auctions for new frequencies, manages frequency bands worldwide (WRC, World Radio Conferences)

<table>
<thead>
<tr>
<th>Mobile phones</th>
<th>Europe (CEPT/ETSI)</th>
<th>USA (FCC)</th>
<th>Japan</th>
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</thead>
<tbody>
<tr>
<td><strong>NMT</strong></td>
<td>453-457 MHz, 463-467 MHz</td>
<td>AMPS, TDMA, CDMA</td>
<td>PDC</td>
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<tr>
<td><strong>GSM</strong></td>
<td>890-915 MHz, 935-960 MHz, 1710-1785 MHz, 1805-1880 MHz</td>
<td>824-849 MHz, 869-894 MHz</td>
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<tr>
<td><strong>TDMA, CDMA, GSM</strong></td>
<td>1850-1910 MHz, 1930-1990 MHz</td>
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<tr>
<th>Cordless telephones</th>
<th>Europe (CEPT/ETSI)</th>
<th>USA (FCC)</th>
<th>Japan</th>
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<tr>
<td><strong>CT1</strong></td>
<td>885-887 MHz, 930-932 MHz</td>
<td>PACS 1850-1910 MHz, 1930-1990 MHz</td>
<td>PHS</td>
</tr>
<tr>
<td><strong>CT2</strong></td>
<td>864-868 MHz</td>
<td>1850-1910 MHz, 1930-1990 MHz</td>
<td>JCT</td>
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<tr>
<td><strong>DECT</strong></td>
<td>1880-1900 MHz</td>
<td>PACS-UB 1910-1930 MHz</td>
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<th>Wireless LANs</th>
<th>Europe (CEPT/ETSI)</th>
<th>USA (FCC)</th>
<th>Japan</th>
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<tr>
<td><strong>IEEE 802.11</strong></td>
<td>2400-2483 MHz</td>
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</tr>
<tr>
<td><strong>HIPERLAN 1</strong></td>
<td>5176-5270 MHz</td>
<td>2400-2483 MHz</td>
<td>2471-2497 MHz</td>
</tr>
</tbody>
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Periodic Signals

- \( g(t) = A_t \sin(2\pi f_t t + \varphi_t) \)

- Amplitude \( A \)
- frequency \( f \) [Hz = 1/s]
- period \( T = 1/f \)
- wavelength \( \lambda \)
  with \( \lambda f = c \)
  \((c=3\cdot10^8 \text{ m/s})\)
- phase \( \varphi \)

- \( \varphi^* = -\varphi T/2\pi [+T] \)
Transmitting digital data: Fourier?

- Every (periodic) signal can be represented by infinitely many sinuses and cosines

\[ g(t) = \frac{1}{2} c + \sum_{n=1}^{\infty} a_n \sin(2\pi n ft) + \sum_{n=1}^{\infty} b_n \cos(2\pi n ft) \]

- But in wireless communication we only have narrow bands
- Also different frequencies behave differently
- Modulation
Antennas: isotropic radiator

- Radiation and reception of electromagnetic waves, coupling of wires to space for radio transmission
- Isotropic radiator: equal radiation in all three directions
- Only a theoretical reference antenna
- Radiation pattern: measurement of radiation around an antenna
- Sphere: $S = 4\pi r^2$

\[ \begin{align*}
\text{ideal isotropic radiator}
\end{align*} \]
Antennas: simple dipoles

- Real antennas are not isotropic radiators but, e.g., dipoles with lengths $\lambda/2$ as Hertzian dipole or $\lambda/4$ on car roofs or shape of antenna proportional to wavelength

- Example: Radiation pattern of a simple Hertzian dipole
Antennas: directed and sectorized

- Often used for microwave connections or base stations for mobile phones (e.g., radio coverage of a valley)

![Directed Antenna](image)

![Sectorized Antenna](image)

**Directed Antenna**

**Sectorized Antenna**
Antennas: diversity

- Grouping of 2 or more antennas
  - multi-element antenna arrays
- Antenna diversity
  - switched diversity, selection diversity
    - receiver chooses antenna with largest output
  - diversity combining
    - combine output power to produce gain
    - cophasing needed to avoid cancellation
Signal propagation ranges

- Propagation in free space always like light (straight line)
- Transmission range
  - communication possible
  - low error rate
- Detection range
  - detection of the signal possible
  - no communication possible
- Interference range
  - signal may not be detected
  - signal adds to the background noise
Attenuation by distance

- Attenuation [dB] = 10 \log_{10} (\text{transmitted power} / \text{received power})
- Example: factor 2 loss = 10 \log_{10} 2 \approx 3 \text{ dB}

- In theory/vacuum (and for short distances), receiving power is proportional to $1/d^2$, where $d$ is the distance.
- In practice (for long distances), receiving power is proportional to $1/d^\alpha$, $\alpha = 4\ldots6$. We call $\alpha$ the path loss exponent.

- Example: Short distance, what is the attenuation between 10 and 100 meters distance? Factor 100 ($=100^2/10^2$) loss = 20 dB
Attenuation by objects

- Shadowing (3-30 dB):
  - textile (3 dB)
  - concrete walls (13-20 dB)
  - floors (20-30 dB)
- reflection at large obstacles
- scattering at small obstacles
- diffraction at edges
- fading (frequency dependent)
Real World Examples
Multipath propagation

- Signal can take many different paths between sender and receiver due to reflection, scattering, diffraction

- Time dispersion: signal is dispersed over time
- Interference with “neighbor” symbols: Inter Symbol Interference (ISI)
- The signal reaches a receiver directly and phase shifted
- Distorted signal depending on the phases of the different parts
Effects of mobility

- Channel characteristics change over time and location
  - signal paths change
  - different delay variations of different signal parts
  - different phases of signal parts
- quick changes in power received (short term fading)

- Additional changes in
  - distance to sender
  - obstacles further away
- slow changes in average power received (long term fading)

- Doppler shift: Random frequency modulation
Multiplexing

- Multiplex channels \( (k) \) in four dimensions
  - space \( (s) \)
  - time \( (t) \)
  - frequency \( (f) \)
  - code \( (c) \)

- Goal: multiple use of a shared medium

- Important: guard spaces needed!

- Example: radio broadcast
Example for space multiplexing: Cellular network

- Simplified hexagonal model

- Signal propagation ranges:
  Frequency reuse only with a certain distance between the base stations

- Can you reuse frequencies in distance 2 or 3 (or more)?

- Graph coloring problem

- Example: fixed frequency assignment for reuse with distance 2

- Interference from neighbor cells (other color) can be controlled with transmit and receive filters
Carrier-to-Interference / Signal-to-Noise

- Digital techniques can withstand a Carrier-to-Interference ratio of approximately 9 dB.

- Assume the path loss exponent $\alpha = 3$. Then,

$$\frac{C}{I} = \frac{(D - R)^\alpha}{R^\alpha} = \left(\frac{D}{R} - 1\right)^\alpha$$

which gives $D/R = 3$. Reuse distance of 2 might just work…

- Remark: Interference that cannot be controlled is called noise. Similarly to $C/I$ there is a signal-to-noise ratio $S/N$ (SNR).
Frequency Division Multiplex (FDM)

- Separation of the whole spectrum into smaller frequency bands
- A channel gets a certain band of the spectrum for the whole time
  + no dynamic coordination necessary
  + works also for analog signals
  - waste of bandwidth if traffic is distributed unevenly
  - inflexible

- Example:
  broadcast radio
Time Division Multiplex (TDM)

- A channel gets the whole spectrum for a certain amount of time
  + only one carrier in the medium at any time
  + throughput high even for many users
    - precise synchronization necessary

- Example: Ethernet
Time and Frequency Division Multiplex

- Combination of both methods
- A channel gets a certain frequency band for some time
  - protection against frequency selective interference
  - protection against tapping
  - adaptive
  - precise coordination required

- Example: GSM
Code Division Multiplex (CDM)

- Each channel has a unique code
- All channels use the same spectrum at the same time
  + bandwidth efficient
  + no coordination or synchronization
  + hard to tap
  + almost impossible to jam
  - lower user data rates
  - more complex signal regeneration
- Example: UMTS
- Spread spectrum
- U. S. Patent 2,292,387, Hedy K. Markey (a.k.a. Lamarr or Kiesler) and George Antheil (1942)
Cocktail party as analogy for multiplexing

• Space multiplex: Communicate in different rooms

• Frequency multiplex: Use soprano, alto, tenor, or bass voices to define the communication channels

• Time multiplex: Let other speaker finish

• Code multiplex: Use different languages and hone in on your language. The “farther apart” the languages the better you can filter the “noise”: German/Japanese better than German/Dutch. Can we have orthogonal languages?
Spread spectrum technology

- Problems: narrowband interference and frequency dependent fading
- Solution: spread the narrow band signal into a broad band signal using a special code

- Side effects: co-existence of several signals, and more tap-proof
- Alternatives: Frequency Hopping or Direct Sequence
Frequency Hopping Spread Spectrum (FHSS)

- Discrete changes of carrier frequency
  - sequence of frequency changes determined via pseudo random number sequence
- Two variants
  - Fast Hopping: several frequencies per user bit
  - Slow Hopping: several user bits per frequency

+ frequency selective fading and interference limited to short period
+ simple implementation
+ uses only small portion of spectrum at any time
  - not very robust
  - frequency hopping has overhead

- Example: Bluetooth
Code Division Multiple Access (CDMA)

- (Media Access Layer – could as well be in Lecture 3)
- As example for Direct Sequence Spread Spectrum (DSSS)
- Each station is assigned an m-bit code (or chip sequence)
- Typically m = 64, 128, ... (in our examples m = 4, 8, ...)
- To send 1 bit, station sends chip sequence
- To send 0 bit, station sends complement of chip sequence

- Example: 1 MHz band with 100 stations
- FDM
  - each station a 10 kHz band
  - assume that you can send 1 bit/Hz: 10 kbps
- CDMA
  - each station uses the whole 1 MHz band
  - less than 100 chips per channel: more than 10 kbps
CDMA basics 1

Each station $s$ has unique $m$-bit chipping code $S$ or complement $\bar{S}$

Bipolar notation: binary 0 is represented by $-1$ (or short: $-$)

Two chips $S, T$ are orthogonal iff $S \cdot T = 0$

$S \cdot T$ is the inner (scalar) product: $S \cdot T = \frac{1}{m} \sum_{i=1}^{m} S_i T_i$

Note: $S \cdot S = 1, S \cdot \bar{S} = -1$

Note: $S \cdot T = 0 \implies S \cdot \bar{T} = 0$
CDMA basics 2

• Assume that all stations are perfectly synchronous
• Assume that all codes are pair wise orthogonal
• Assume that if two or more stations transmit simultaneously, the bipolar signals add up linearly

• Example
• $S = (+ - + - + - + -)$
• $T = (+ + - - - + + -)$
• $U = (+ - - + - - + +)$
• Check that codes are pair wise orthogonal
• If $S, T, U$ send simultaneously, a receiver receives
$R = S + T + U = (+3, -1, -1, -1, -1, -1, +3, -1)$
CDMA basics 3

• To decode a received signal $R$ for sender $s$, one needs to calculate the normalized inner product $R \cdot S$.

• $R \cdot S = (+3, -1, -1, -1, -1, 3, -1) \cdot (+ - + - + -)$
  $= (+3+1-1+1-1+1+3+1)/8$
  $= 8/8 = 1 \ldots$ by accident?

• $R \cdot S = (S+T+U) \cdot S = S \cdot S + T \cdot S + U \cdot S = 1 + 0 + 0 = 1$

• With orthogonal codes we can safely decode the original signals
CDMA: How much noise can we tolerate?

- We now add random noise to before we receive the signal:
  \[ R' = R + N, \text{ where } N \text{ is an } m\text{-digit noise vector}. \]

- Assume that chipping codes are balanced (as many “+” as “−”)
- If \( N = (\alpha, \alpha, \ldots, \alpha) \) for any (positive or negative) \( \alpha \), then the noise \( N \) will not matter when we decode the received signal.

- \( R' \cdot S = (R+N) \cdot S = S \cdot S + (\text{orthogonal codes}) \cdot S + N \cdot S = 1 + 0 + 0 = 1 \)

- How much random (white) noise can we tolerate? (See exercises)
CDMA: Construction of orthogonal codes with $m$ chips

- Note that we cannot have more than $m$ orthogonal codes with $m$ chips because each code can be represented by a vector in the $m$-dimensional space, and there are not more than $m$ orthogonal vectors in the $m$-dimensional space.

- Walsh-Hadamard codes can be constructed recursively (for $m = 2^k$):

  The set of codes of length 1 is $C_0 = \{ (+ ) \}$.

  For each code $(c)$ $\in$ $C_k$ we have two codes $(c c)$ and $(c \overline{c})$ in $C_{k+1}$.

- Code tree:

  $C_0 = \{ (+ ) \}$

  $C_1 = \{ (+ +), (+ -) \}$

  $C_2 = \{ (+ + + +), (+ + - -), (+ - + -), (+ - - +) \}$
CDMA: Random codes

- We cannot have more than $m$ orthogonal codes.

- Martin Cooper (Motorola, right) says “… with UMTS you get at most 1 Mbps …”, the Swiss newspaper Sonntagszeitung adds “… but when you have to share a cell with 12 [16?] others, you get at most 64 kbps.”

- We said: “100 stations … with less than 100 chips per [station]”

- Idea: Random codes are almost balanced and almost pair wise orthogonal
CDMA: Random codes 2

- With \( k \) other stations, and \( m \) chips
- \( m \cdot R \cdot S = m \cdot S \cdot S + m \cdot (k \text{ random codes}) \cdot S = \pm m + X \), where \( X \) is the sum of \( mk \) random variables that are either +1 or –1.
- Since the random variables are independent, the expected value of \( X \) is 0. And better: The probability that \( X \) is “far from 0” is “small.”
- Therefore we may decode the signal as follows:
  \( R \cdot S > \varepsilon \) \( \implies \) decode 1; \( R \cdot S < -\varepsilon \) \( \implies \) decode 0. What if \( -\varepsilon \leq R \cdot S \leq \varepsilon \)?
- Experimental evaluation (right): For \( k = m = 128 \) decoding is correct more than 80%. But more importantly: Even if \( k > m \) (\( k=1..500 \)), the system does not deteriorate quickly.
CDMA: Problems

Some of our assumptions were not accurate:

A) It is not possible to synchronize chips perfectly. What can be done is that the sender first transmits a long enough known chip sequence on which the receiver can lock onto.

B) Not all stations are received with the same power level. CDMA is typically used for systems with fixed base stations. Then mobile stations can send with the reciprocal power they receive from the base station. (Alternatively: First decode the best station, and then subtract its signal to decode the second best station?)

C) We still didn’t discuss how to transmit bits with electromagnetic waves.
CDMA: Summary

+ all terminals can use the same frequency, no planning needed
+ reduces frequency selective fading and interference
+ base stations can use the same frequency range
+ several base stations can detect and recover the signal
+ soft handover between base stations
+ forward error correction and encryption can be easily integrated
  – precise power control necessary
  – higher complexity of receiver and sender

Modulation and demodulation

Digital data 101101001

- Digital modulation
- Analog baseband signal

- Analog modulation
- Radio carrier

Radio transmitter

Radio receiver

- Analog demodulation
- Analog baseband signal

- Synchronization decision
- Digital data 101101001

- Radio carrier
Digital modulation

- Modulation of digital signals known as Shift Keying

- Amplitude Shift Keying (ASK):
  - very simple
  - low bandwidth requirements
  - very susceptible to interference

- Frequency Shift Keying (FSK):
  - needs larger bandwidth

- Phase Shift Keying (PSK):
  - more complex
  - robust against interference
Different representations of signals

- For many modulation schemes not all parameters matter.
Advanced Frequency Shift Keying

- MSK (Minimum Shift Keying)

- bandwidth needed for FSK depends on the distance between the carrier frequencies
- Avoid sudden phase shifts by choosing the frequencies such that (minimum) frequency gap \( \delta f = 1/4T \) (where \( T \) is a bit time)
- During \( T \) the phase of the signal changes continuously to \( \pm \pi \)

- Example GSM: GMSK (Gaussian MSK)
Advanced Phase Shift Keying

- **BPSK (Binary Phase Shift Keying):**
  - bit value 0: sine wave
  - bit value 1: inverted sine wave
  - Robust, low spectral efficiency
  - Example: satellite systems

- **QPSK (Quadrature Phase Shift Keying):**
  - 2 bits coded as one symbol
  - symbol determines shift of sine wave
  - needs less bandwidth compared to BPSK
  - more complex

- **Dxxxx (Differential xxxx)**
Modulation Combinations

- Quadrature Amplitude Modulation (QAM)
  - combines amplitude and phase modulation
  - it is possible to code $n$ bits using one symbol
  - $2^n$ discrete levels, $n=2$ identical to QPSK
  - bit error rate increases with $n$, but less errors compared to comparable PSK schemes

- Example: 16-QAM (4 bits = 1 symbol)
  - Symbols 0011 and 0001 have the same phase, but different amplitude.
  - 0000 and 1000 have different phase, but same amplitude.
  - Used in 9600 bit/s modems