







## **Consistency models:**

- Linearizable
- **Sequentially Consistency**
- **Quiescent Consistency**

#### Theorem:

Linearizable implies both sequentially and quiescent consistency.







### Linearizable:

- "one global order"
- Linearizable → put points on a "line"
- Stronges assumption, implies other two







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- Linearizable 

  put points on a "line"
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 write x=1	write x=3		read x=2			
	read x=1	W	rite y=1			
write x=2				read y=1		



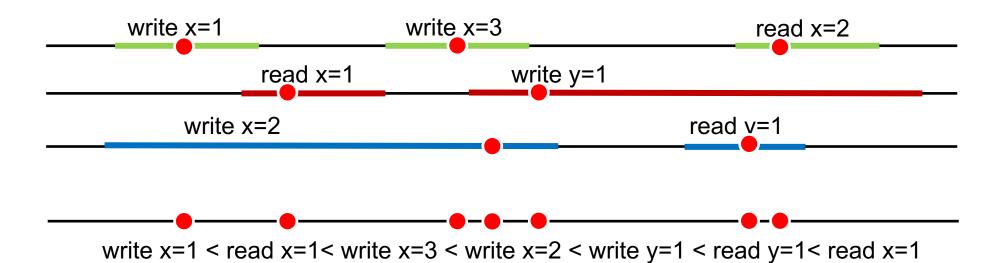




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write x=2		write y=1			
write y=2			read y=2		

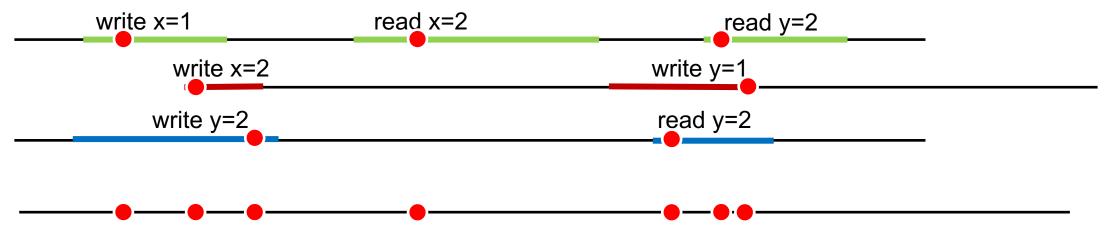






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write x=1 < write <math>x=2 < write y=2 < read x=2 < read y=2 < read y=2 < write y=1







## **Quiscent Consistency**

Synchronizes all threads on quiescent point, i.e. point where no execution happens

		read x=1			read y=1
write x=1				write y=1	
	write x=2		read y=1	_	

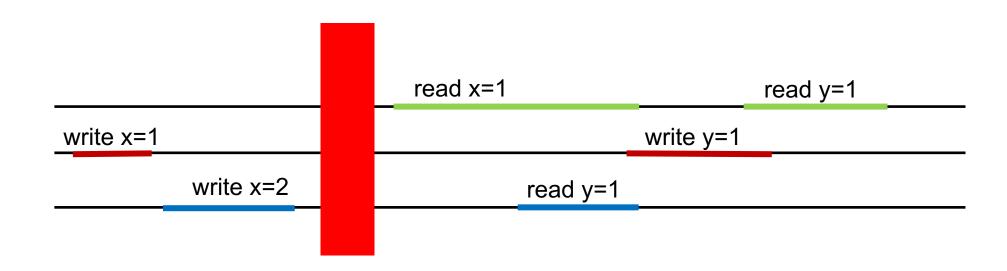






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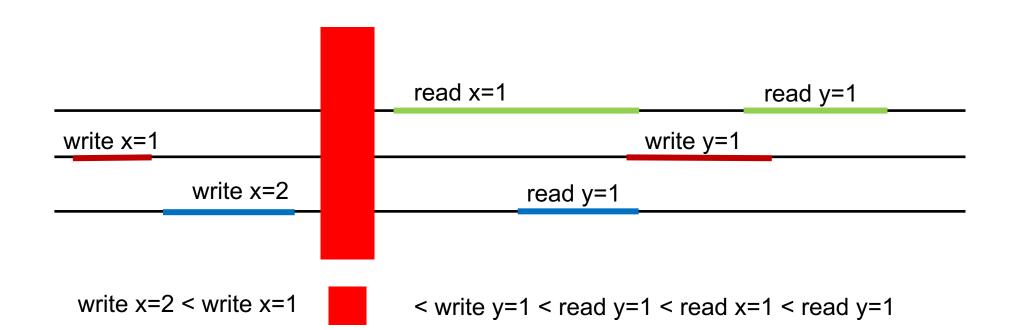






## **Quiscent Consistency**

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# **Composable Consistency**

- Definition: If you only look at all operations concerning any object and the execution is consistent, then also the whole execution is consistent
- Sequentially consistent is not composable
- Linearizability is composable
- Quiescent consistency is composable







## **Composable Consistency**

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# **Logical Clocks:**

- Happened before relation " $\rightarrow$ " holds
  - 1) IF f < g on the same node
  - 2) Send happens before receive
  - 3) If  $f \rightarrow g$  and  $g \rightarrow h$ , then  $f \rightarrow h$  (transitivity)







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# **Logical Clocks:**

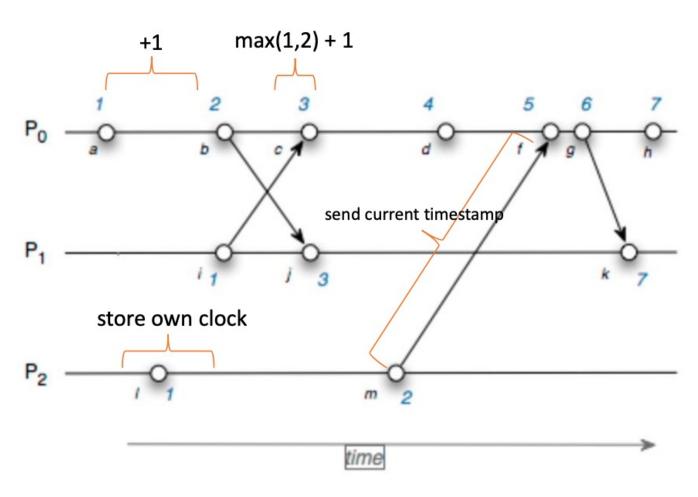
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- C(a): timestamp of event a
- logical clocks:  $a \rightarrow b$  implies c(a) < c(b)
- Strong logical clock: c(a) < c(b) implies  $a \rightarrow b$  (in addition)







# **Lamport Clocks:**

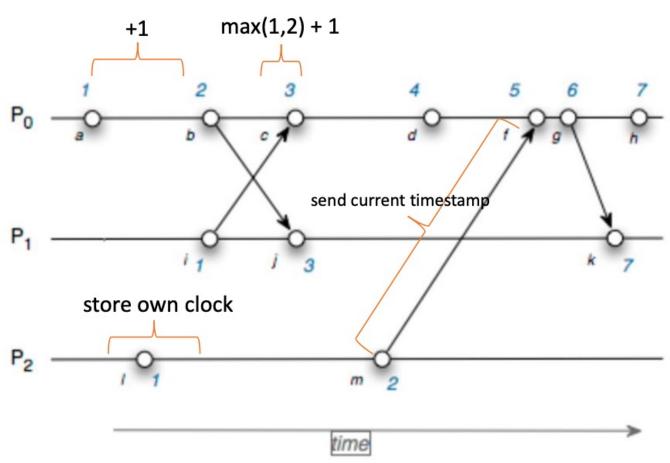








## **Lamport Clocks:**



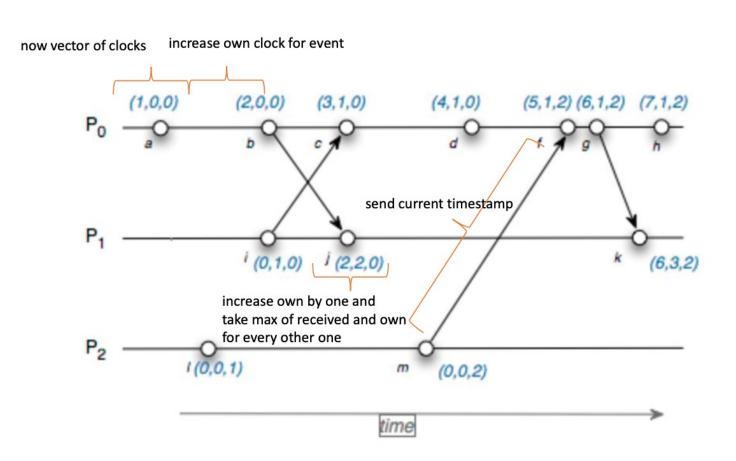
Weak logical clock:  $a \rightarrow b$  implies c(a) < c(b) but not vice versa







### **Vector Clocks:**









#### **Vector Clocks:**

- What does c(a) < c(b) mean now?
  - if all the entries in a<= b and at least one entry where a < b
- Is a **logical clock** (so if a  $\rightarrow$  b then c(a) < c(b))
- Is also a **strong logical clock** (if  $c(a) < c(b) \rightarrow a \rightarrow b$ ) intuitionL because in order to achive c(a) < c(b), all entries have to be at least as big, so a message from a must have reached b (not necessarily directly) so that b has the right value







## **Consistent Snapshot:**

- Cut: prefix of a distributed execution
- **Consistent Snapshot:** 
  - a cut where for every operation h in that cut, if  $f \rightarrow g$ , then the cut contains f
  - if all "connected" preceding operations are included
- With number of consistent snapshots, one can make conclusions about degrees of concurrency in system







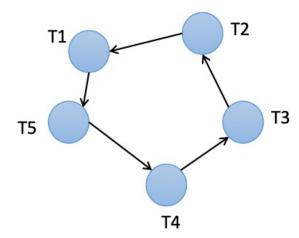
Centralized mutual exclusion







- Centralized mutual exclusion
- Token-based mutual exclusion

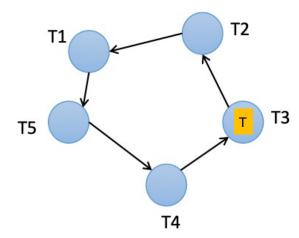








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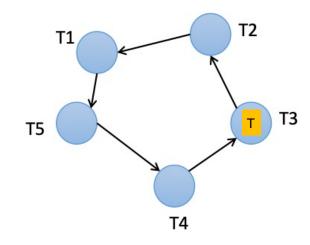








- Centralized mutual exclusion
- Token-based mutual exclusion



$$T = T3$$
?

- enter critical section

- send token to T2

$$- set T = T3$$

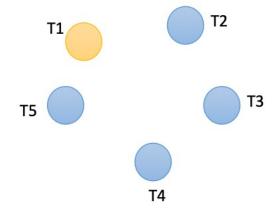
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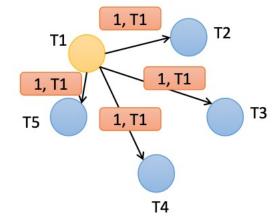
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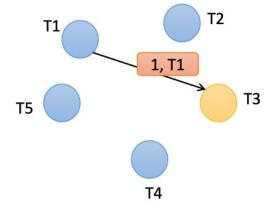








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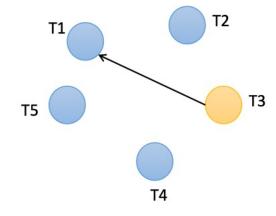








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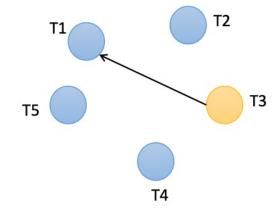
- T3 < T &&want access? defer response
- Else send response







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- T3 < T &&want access? defer response
- Else send response
- All responses received? enter critical section







### **Time & Clocks**

- Wall clock time: "true" time
- clock error

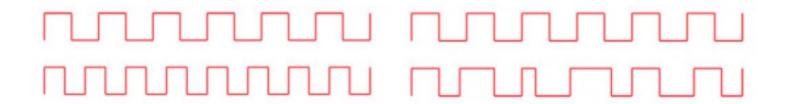


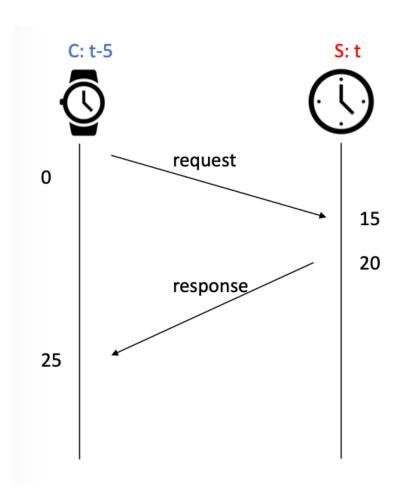
Figure 20.8: Drift (left) and Jitter (right). On top is a square wave, the wallclock time  $t^*$ .







## NTP



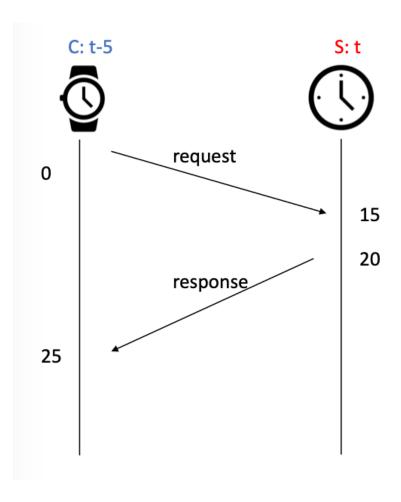
Propagation delay = ((25-0) - (20-15)) / 2 = 10







## NTP



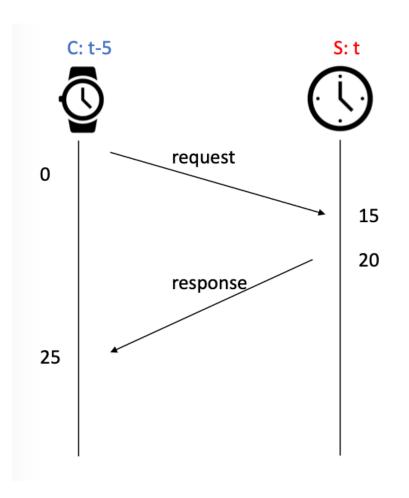
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## **NTP**



Propagation delay = ((25-0) - (20-15)) / 2 = 10Assumed to be symmetric!

Skew = ((15-0) + (20-25))/2 = 5→ Adjus clock by skew







# **Alternative Synchronization Protocols**

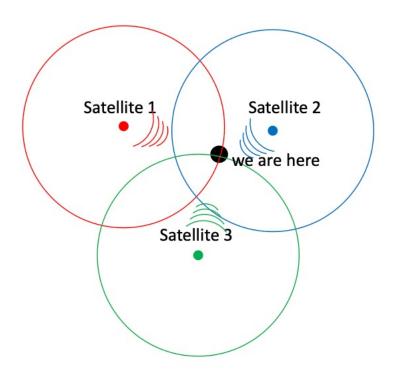
- **Precision Time Protocol**
- **Local Time Synchronization**
- Wireless Clock Synchronization with Known Delays







## **GPS - General Idea**

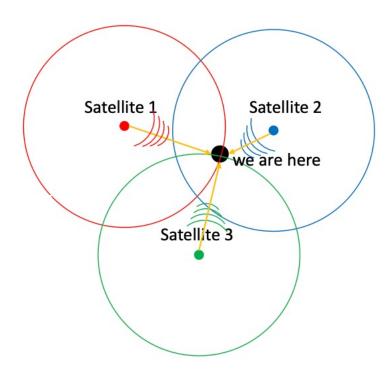








Satellites transmit location and timestamp when sent



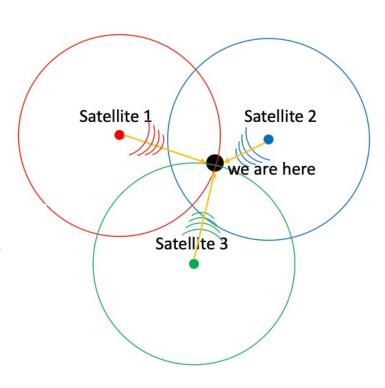






Satellites transmit location and timestamp when sent

→ Compare satellite timestamp to local timestamp and calculate distance



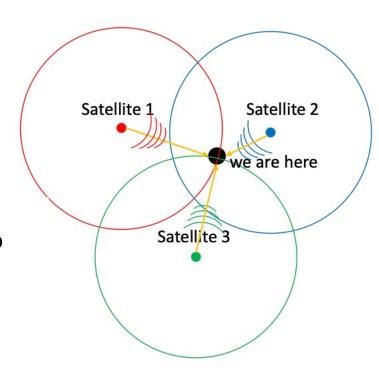






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Problem: Quadratic equation results in two possible locations

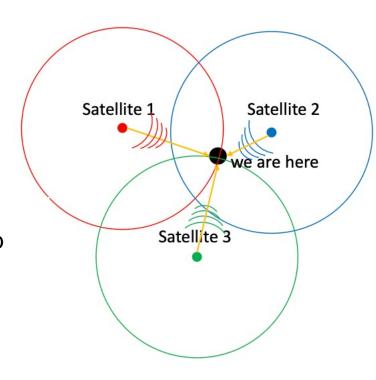






Satellites transmit location and timestamp when sent

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Problem: Quadratic equation results in two possible locations

Solution: Generally, only one close to Earth's surface

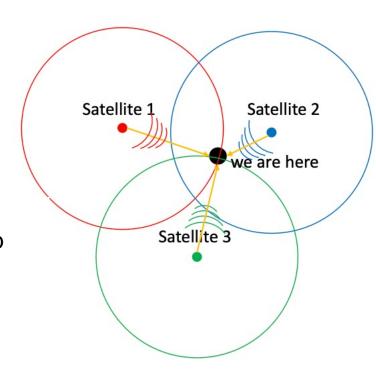






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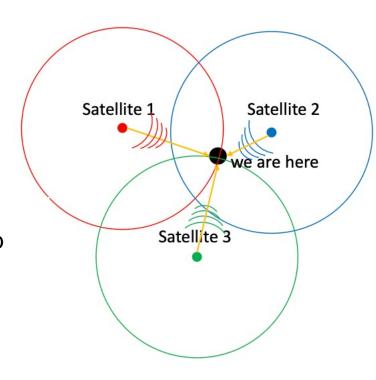






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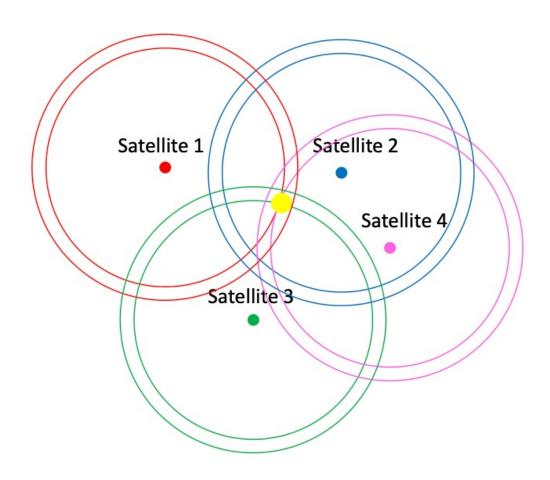
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Solution: take measurements from forth satellite!





# **GPS - Redifined**









Does sequential consistency imply quiescent consistency?

2. Are there guarantees a Lamport clock can achieve a vector clock cannot?

Does a high number of consistent snapshots imply a high level of concurrency?







Does sequential consistency imply quiescent consistency? - Wrong



- Are there guarantees a Lamport clock can achieve a vector clock cannot? No, because the concept of a Lamport clock is included in the vector clock concept
- Does a high number of consistent snapshots imply a high level of concurrency? - True







4. What is the difference between jitter and drift?







4. What is the difference between jitter and drift?







### Clock Sync

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### **Clock Synchronization**

- a) Assume you run NTP to synchronize speakers in a soccer stadium. Each speaker has a radio downlink to receive digital audio data. However, there is no uplink! You decide to use an acoustic signal transmit by the speaker. To synchronize its clock, a speaker first plays back an acoustic signal. This signal is picked up by the NTP server which responds via radio. The speaker measures the exact time that passes between audio playback and radio downlink response. What is likely the largest source of error?
- b) What are strategies to reduce the effect of this error source?
- c) Prove or disprove the following statement: If the average local skew is smaller than x, then so is the average global skew.
- d) Prove or disprove the following statement: If the average global skew is smaller than x, then so is the average local skew.







#### Time Difference of Arrival

Assume you are located on a line y = -x + 8 km in the two dimensional plane. You receive the GPS signals from satellites A and B. Both signals are transmitted exactly at the same time t by both satellites. You receive the signal from satellite A 3.3  $\mu$ s before the signal of satellite B. At time t, satellite A is located at  $p_A = (6 \text{ km}, 6 \text{ km})$  and satellite B is located at  $p_B = (2 \text{ km}, 1 \text{ km})$ , in the plane.

- a) Formulate the least squares problem to find your location.
- b) Are you more likely to be at position (2 km, 6 km) or (4 km, 4 km)?
- c) What is the time when receiving the signal from satellite B?







### Clock Synchronization: Spanning Tree

Common clock synchronization algorithms (e.g. TPSN, FTSP) rely on a spanning tree to perform clock synchronization. Finding a good spanning tree for clock synchronization is not trivial. Nodes which are neighbors in the network graph should also be close-by in the resulting tree. Show that in a grid of  $n = m \times m$  nodes there exists at least a pair of nodes with a stretch of at least m. The stretch is defined as the hop distance in the tree divided by the distance in the grid.







### NTP Programming

Write a Linux program that prints the current UTC time and the maximum error.

**Hint:** Have a look at the manpage for adjtimex.







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### Consistency and Logical Clocks

Quiz	
<b>4</b> 3111	

#### Different Consistencies

Prove or disprove the following statements:

- a) Neither sequential consistency nor quiescent consistency imply linearizability.
- b) If a system has sequential consistency and quiescent consistency, it is linearizable.







#### Measure of Concurrency from Vector Clocks

You are given two nodes that each have a vector logical clock that additionally logs the clock state upon receiving a message (see Algorithm 1).

#### Algorithm 1 Vector clocks with logging

- 1: (Code for node u)
- 2: Initialize  $c_u[v] := 0$  for all other nodes v.
- 3: Upon local operation: Increment current local time  $c_u[u] := c_u[u] + 1$ .
- 4: Upon send operation: Increment  $c_u[u] := c_u[u] + 1$  and include the whole vector  $c_u$  as d in message.
- 5: Upon receive operation: Extract vector d from message and update  $c_u[v] := \max(d[v], c_u[v])$ for all entries v. Increment  $c_u[u] := c_u[u] + 1$ . Save the vector  $c_u$  to the log file of node u.

Assume that exactly one message gets send from one to the other node. Given the logs and current vector states of both nodes, write a short program that calculates the measure of concurrency as defined in the script (Definition 19.30). You can use your favorite programming language. The example solution will be in Python.

#### Advanced

Generalize your program to any number of messages exchanged between the nodes.