

$$L_3 = \{w \mid \#_{01}(w) = \#_{10}(w)\}$$

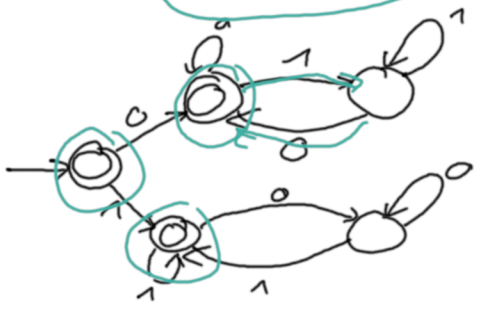
$$\Sigma = \{0, 1\}$$

$$\Delta \leq 1$$

$$+1 \#_{01}$$

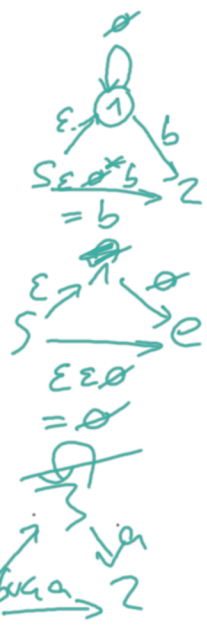
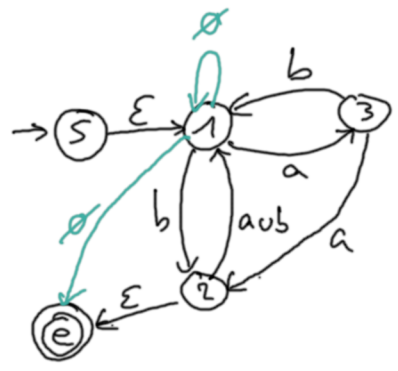
$$+ \#_{10}$$

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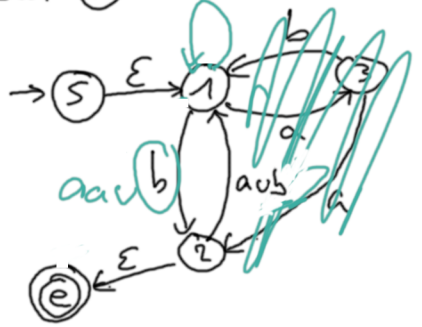


Exercise 1:

GNFA:



rip out (3)

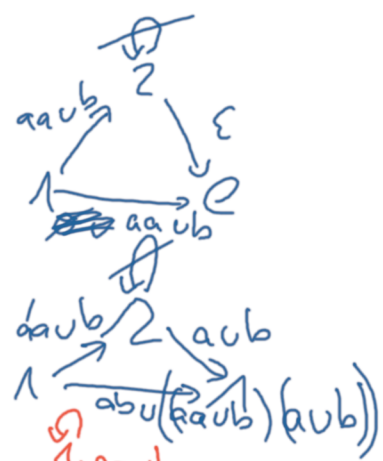
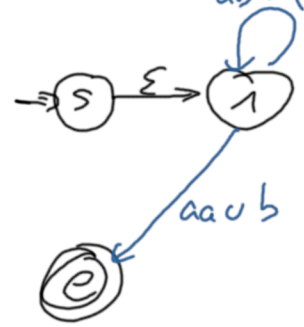


$$a \rightarrow 3 \xrightarrow{b} 1$$

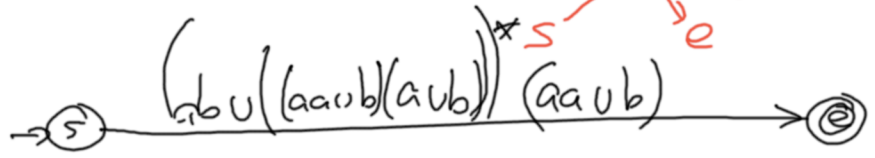
$$1 \xrightarrow{a} 3 \xrightarrow{b} 1$$

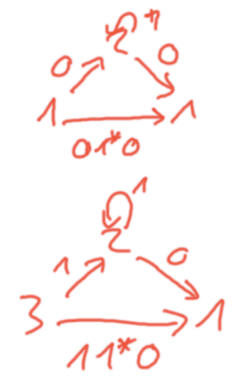
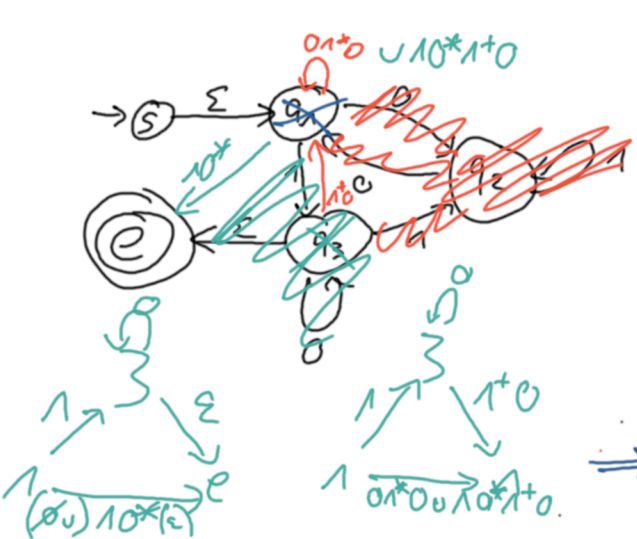
$$= ab$$

rip out (2)  $ab \cup (aab)(aub)$



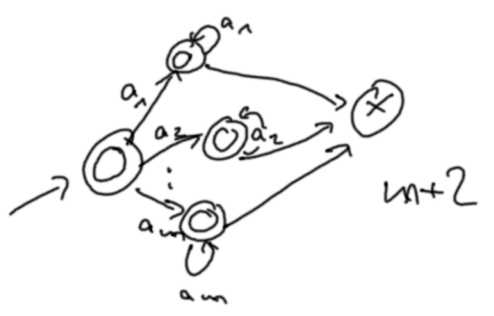
rip out (1):





$$\Rightarrow \text{REG} = (01^*0 \cup 10^*1+0)^* 10^*$$

$$a_1^* \cup a_2^* \cup a_3^* \cup \dots \cup a_m^* \quad a_i \in \Sigma$$



~~$L_1 = 1^*0^*$~~   ~~$L_2 = 1^*$~~   
 ~~$L = L_1 \cup L_2 = 1^*0^* \cup 1^*$~~

$$L_1 = 1^*0^*1^*0^* \Rightarrow p_1 \leq 3$$

$$L_2 = 1^*1^*0^* \Rightarrow p_2 \geq 4$$

$$L = L_1 \cup L_2 \Rightarrow p \leq \max\{p_1, p_2\}$$

110 not pumpable in L  
 $\Rightarrow p > 4, p \leq 5$

$p_2 = 4 \Rightarrow w = 1110$  pumpable  
 $\Rightarrow xy^iz \dots xz \dots \notin L$

$1^*0^*1^*0^*$   
~~1~~, ~~101~~, ~~001~~, ~~011~~, ~~011~~  
 0100000