ETH
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Distributed
Computing

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Computational Thinking
Exercise 5 (Cryptography)

1 Nonce Reuse

In the ElGamal digital signature scheme, why should the same random nonce never be reused for 2 different messages with the same public/secret keypair?

2 Cryptographic Hash Functions

Let $h_1, h_2 : \{0,1\}^* \rightarrow \{0,1\}^n$ be two collision resistant functions. Are the following hash functions also collision resistant? Explain[1].

- $h_3(x) = h_1(x) \oplus h_2(x)$
- $h_4(x) = x_0; h_1(x)$

Hint: Try to find a collision or reduce the collision-resistance of the constructed hash functions to collision-resistance of h_1 and h_2.

3 ElGamal Encryption

In the lecture we have have shown that: CDH $\leq$ Breaking-ElGamal-Encryption. Show that Breaking-ElGamal-Encryption $\leq$ CDH.

4 Active Adversary in ElGamal Encryption

Alice wants to bid an amount of money ($2k$\$) in an auction[2]. To do this, Alice sends the amount of money she is bidding securely by using the ElGamal-Encryption scheme.

a) Show that ElGamal Encryption scheme is homomorphic.

b) Use this property to reduce the amount of money that Alice is bidding by half (i.e. to k\$).

c) How can Alice prevent this attack?

[1] x_0 means the first bit of the message x, and as in the lecture, concatenation of messages is denoted by ;

[2] For example, in Ebay.