# ETH

Eidgenössische Technische Hochschule Zürich Swiss Federal Institute of Technology Zurich

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Distributed Computing



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## **Distributed Systems Part II**

Solution to Exercise Sheet 1

#### An Asynchronous Riddle 1

- a) The crucial idea is to select one prisoner as a leader. The leader will turn the switch off, whenever he enters the room and the switch is on. All other prisoner will turn the switch on exactly once. So a prisoner who enters the room looks at the switch. If the switch is off and the prisoner has never turned it on before, he will turn the switch on. If the switch is already on or the prisoner already did turn the switch on during an earlier visit, he leaves the switch as it was. The leader counts how many times he turns the switch off. If the leader counted 99 times he can declare "We all visited the switch room at least once". Because he knows, that each of the other 99 prisoners has turned the switch on and he himself has been in the room as well.
- **b**) If the initial position of the switch is unknown, the above protocol cannot be used, since the leader may miscount by one. However, this can easily be fixed. If each prisoner turns the switch on exactly twice, the leader can be sure that everyone visited the room after counting up to  $2 \cdot 99 = 198$  turns.

#### $\mathbf{2}$ **Communication Models**

Some ideas are:

- **Delay** There is no delay with shared memory, if one process writes the other processes can read immediately. With messsage passing delay can happen (not necessarily in every model), different messages may even have different delays.
- **Overriding** With shared memory if a process writes to a register, another process may override the value before anyone could read the register. In message passing this cannot happen. On the other hand messages may be lost, or the inbox buffer of a process may overflow, leading to similar results.
- **Consistency** With message passing several message may be sent at the same time, and the order of arriving message may be messed up. With shared memory the value of a register is always the value that was written last.

### 3 Consensus with an n-Register

We require 6 registers. We call the first three registers  $R_0$ ,  $R_1$  and  $R_2$ . To the other three registers we give the names  $R_{\{0,1\}}$ ,  $R_{\{0,2\}}$  and  $R_{\{1,2\}}$ . The goal is to find the *fastest* process and take its input value as decision. In words, the protocol works as follows:

In a single step process i writes its id into  $R_i$  and into  $R_{\{i,j\}}$  for  $i \neq j$ .

It then checks for all  $i \neq j$  whether process *i* was faster than process *j*:

If  $R_{\{i,j\}} = -1$  then neither *i* nor *j* have yet done anything.

Otherwise, if  $R_i = -1$  then process j must be faster than i.

Otherwise, if  $R_j = -1$  then process *i* must be faster than *j*.

Otherwise  $R_{\{i,j\}}$  holds the id of the process which was slower.

With all this information, a process can calculate which process must have been the fastest.

### Solution in pseudo code:

```
initialize(){
  // R are the shared registers
  R[] = [-1, -1, -1, -1, -1];
  // the input, an array of length 3
  \operatorname{input}[] = [\operatorname{random}(), \operatorname{random}(), \operatorname{random}()];
}
decide(){
  id = this.getThreadId();
  // the identifiers of the other processes
  others = [\{0, 1, 2\} \text{ without } \{id\}];
  // atomically write three registers
  write (R[id] = id, R[id, others[0]] = id, R[id, others[1]] = id);
  // pairwise comparison of process-speed
  fastest01 = faster(0, 1, id);
  fastest02 = faster(0, 2, id);
  fastest12 = faster(1, 2, id);
  // find the process which is faster than all the others
  score [] = [0, 0, 0];
  score [fastest01] = score [fastest01]+1;
  score [fastest02] = score [fastest02] + 1;
  score[fastest12] = score[fastest12]+1;
  winner = \max(\text{ score });
  if ( \operatorname{count} [0] = \operatorname{winner} )
    decision = input [0]
  else if ( \operatorname{count} [1] = \operatorname{winner} )
    decision = input [1];
  else // count[2] = winner
    decision = input [2];
}
faster(i, j, id)
```

```
somethingHappened = true;
while (somethingHappened) {
  //\ensuremath{\,\mathrm{We}} need to assure, that we read a consistent memory state
  // This is still wait-free, this loop is traversed at most 3 times
  rij = R[i, j]; ri = R[i]; rj = R[j];
  rijSecond = R[i,j]; riSecond = R[i]; rjSecond = R[j];
  if(rij == rijSecond && ri == riSecond && rj == rjSecond) {
    somethingHappened = false;
  }
}
if (rij = -1) \{ // neither of i or j yet started, I am faster than both
  return id;
}
else{
   if ( ri == -1 ){
  // i did not yet start, hence j must be faster
  return j;
  }
  if ( rj == -1 ){
    // j did not yet start, hence i must be faster
    return i;
  }
  if(rij == i)
    // value written by j was overridden by i
    return j;
  }
  else{ // rj == j
    return i;
  }
}
```

}