

# Inventory Tracking (Cargo Tracking)

- Current tracking systems require lineof-sight to satellite.
- Count and locate containers
- Search containers for specific item
- Monitor accelerometer for sudden motion
- Monitor light sensor for unauthorized entry into container

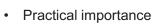


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# Rating

Area maturity

First steps



No apps

Mission critical

Text book

· Theoretical importance

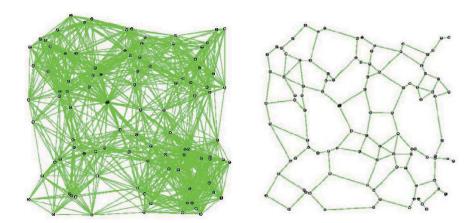
Booooooring

Exciting

# Overview - Topology Control

- Proximity Graphs: Gabriel Graph et al.
- Practical Topology Control: XTC
- Interference

### **Topology Control**



- Drop long-range neighbors: Reduces interference and energy!
- But still stay connected (or even spanner)

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# Gabriel Graph

**Network Connectivity** 

**Spanner Property** 

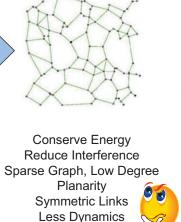
 $d_{TC}(u,v) \leq t \cdot d(u,v)$ 

 Let disk(u,v) be a disk with diameter (u,v) that is determined by the two points u,v.

Topology Control as a Trade-Off

**Topology Control** 

- The Gabriel Graph GG(V) is defined as an undirected graph (with E being a set of undirected edges). There is an edge between two nodes u,v iff the disk(u,v) including boundary contains no other points.
- As we will see the Gabriel Graph has interesting properties.

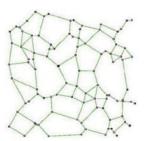


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### **Spanners**

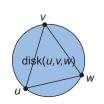
- Let the distance of a path from node u to node v, denoted as d(u,v), be the sum of the Euclidean distances of the links of the shortest path.
  - Writing  $d(u,v)^p$  is short for taking each link distance to the power of p, again summing up over all links.
- Basic idea: S is spanner of graph G if S is a subgraph of G that has certain properties for all pairs of nodes, e.g.
  - Geometric spanner:  $d_S(u,v) \le c \cdot d_G(u,v)$
  - − Power spanner:  $d_S(u,v)^{\alpha} \le c \cdot d_G(u,v)^{\alpha}$ , for path loss exponent α
  - Weak spanner: path of S from u to v within disk of diameter  $c \cdot d_G(u,v)$
  - Hop spanner:  $d_s(u,v)^0 \le c \cdot d_G(u,v)^0$
  - Additive hop spanner:  $d_s(u,v)^0 \le d_G(u,v)^0 + c$
  - $(\alpha, \beta)$  spanner:  $d_s(u,v)^0 \le \alpha \cdot d_G(u,v)^0 + \beta$
  - In all cases the stretch can be defined as maximum ratio d<sub>G</sub>/d<sub>S</sub>

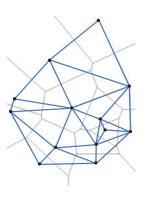




### **Delaunay Triangulation**

- Let disk(u,v,w) be a disk defined by the three points u,v,w.
- The Delaunay Triangulation (Graph)
   DT(V) is defined as an undirected
   graph (with E being a set of undirected
   edges). There is a triangle of edges
   between three nodes u,v,w iff the
   disk(u,v,w) contains no other points.
- The Delaunay Triangulation is the dual of the Voronoi diagram, and widely used in various CS areas; the DT is planar; the distance of a path (s,...,t) on the DT is within a constant factor of the s-t distance.





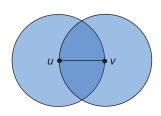
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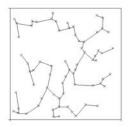
### Other planar graphs

- Relative Neighborhood Graph RNG(V)
  - An edge e = (u,v) is in the RNG(V) iff there is no node w in the "lune" of (u,v), i.e., no noe with with (u,w) < (u,v) and (v,w) < (u,v).</li>



 A subset of E of G of minimum weight which forms a tree on V.





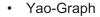
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# Properties of planar graphs

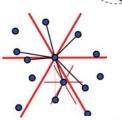
- Theorem 1:
  MST ⊂ RNG ⊂ GG ⊂ DT
- Corollary: Since the MST is connected and the DT is planar, all the graphs in Theorem 1 are connected and planar.
- Theorem 2: The Gabriel Graph is a power spanner (for path loss exponent  $\alpha \geq 2).$  So is GG  $\cap$  UDG.
- Remaining issue: either high degree (RNG and up), and/or no spanner (RNG and down). There is an extensive and ongoing search for "Swiss Army Knife" topology control algorithms.

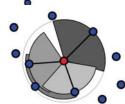
## Overview Proximity Graphs

- β-Skeleton
  - Disk diameters are  $\beta \cdot d(u,v)$ , going through u resp. v
  - Generalizing GG ( $\beta$  = 1) and RNG ( $\beta$  = 2)



- Each node partitions directions in k cones and then connects to the closest node in each cone
- Cone-Based Graph
  - Dynamic version of the Yao Graph. Neighbors are visited in order of their distance, and used only if they cover not yet covered angle





### Lightweight Topology Control

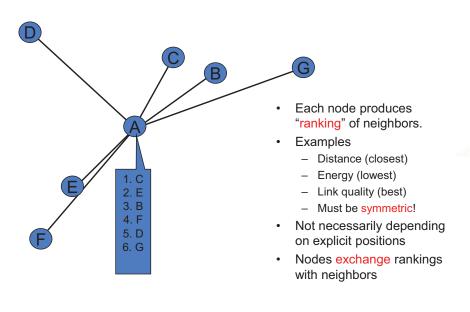
 Topology Control commonly assumes that the node positions are known.

What if we do not have access to position information?



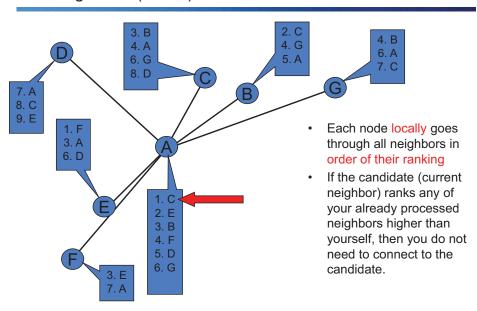
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# XTC: Lightweight Topology Control without Geometry



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### XTC Algorithm (Part 2)



### XTC Analysis (Part 1)

Symmetry: A node u wants a node v as a neighbor if and only if v wants u.

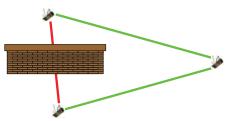
Proof:

 Assume 1) u → v and 2) u ← v
 Assumption 2) ⇒ ∃w: (i) w ≺<sub>v</sub> u and (ii) w ≺<sub>u</sub> v

 Contradicts Assumption 1)

#### XTC Analysis (Part 1)

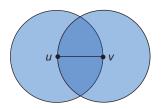
- Symmetry: A node u wants a node v as a neighbor if and only if v wants u.
- Connectivity: If two nodes are connected originally, they will stay so (provided that rankings are based on symmetric link-weights).
- If the ranking is energy or link quality based, then XTC will choose a topology that routes around walls and obstacles.



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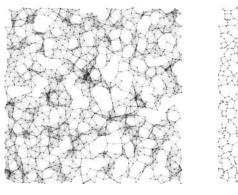
### XTC Analysis (Part 2)

- If the given graph is a Unit Disk Graph (no obstacles, nodes homogeneous, but not necessarily uniformly distributed), then ...
- The degree of each node is at most 6.
- The topology is planar.
- The graph is a subgraph of the RNG.
- Relative Neighborhood Graph RNG(V):
  - An edge e = (u,v) is in the RNG(V) iff there is no node w with (u,w) < (u,v) and (v,w) < (u,v).</li>

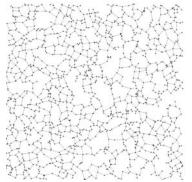


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### XTC Average-Case

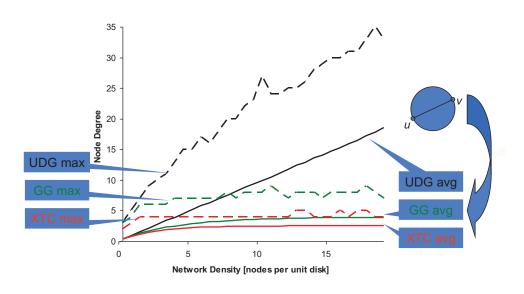


Unit Disk Graph

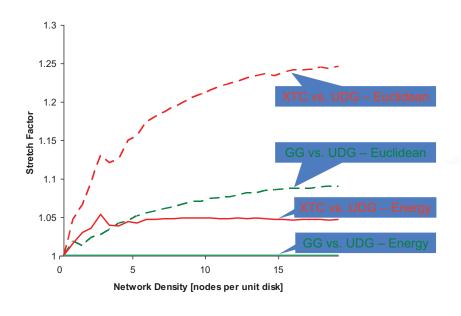


XTC

## XTC Average-Case (Degrees)

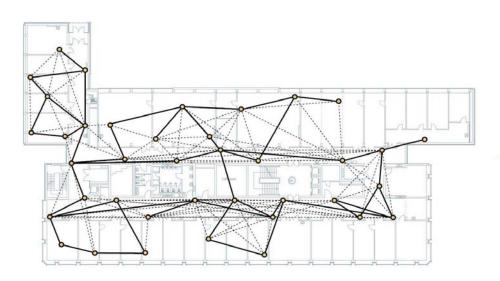


## XTC Average-Case (Stretch Factor)



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## Implementing XTC, e.g. BTnodes v3

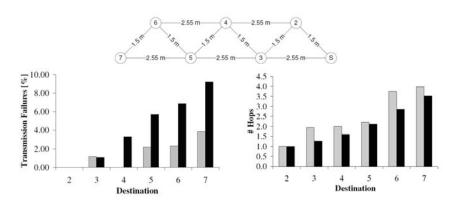


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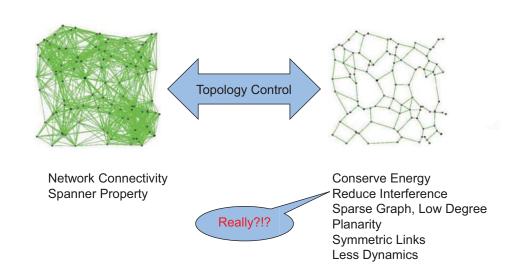
## Implementing XTC, e.g. on mica2 motes

#### · Idea:

- XTC chooses the reliable links
- The quality measure is a moving average of the received packet ratio
- Source routing: route discovery (flooding) over these reliable links only
- (black: using all links, grey: with XTC)



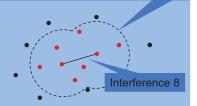
## Topology Control as a Trade-Off



#### What is Interference?

Exact size of interference range does not change the results

Link-based Interference Model



"How many nodes are affected by communication over a given link?"

Node-based Interference Model



"By how many other nodes can a given network node be disturbed?"

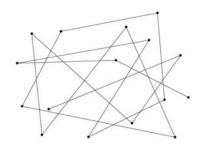
- Problem statement
  - We want to minimize maximum interference
  - At the same time topology must be connected or spanner



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## Low Node Degree Topology Control?

Low node degree does not necessarily imply low interference:

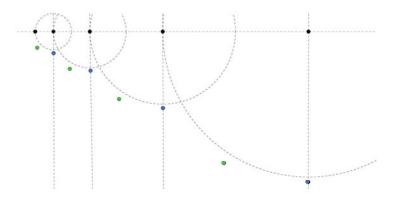


Very low node degree but huge interference

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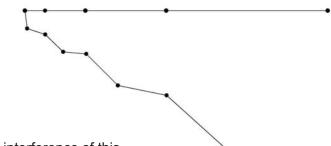
# Let's Study the Following Topology!

...from a worst-case perspective



### Topology Control Algorithms Produce...

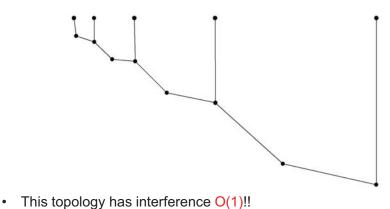
 All known topology control algorithms (with symmetric edges) include the nearest neighbor forest as a subgraph and produce something like this:



 The interference of this graph is Ω(n)!

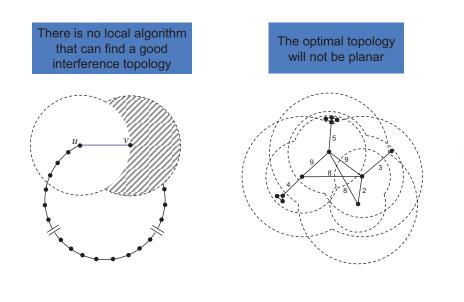
#### But Interference...

Interference does not need to be high...



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#### Link-based Interference Model



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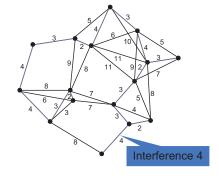
#### Link-based Interference Model

- LIFE (Low Interference Forest Establisher)
  - Preserves Graph Connectivity

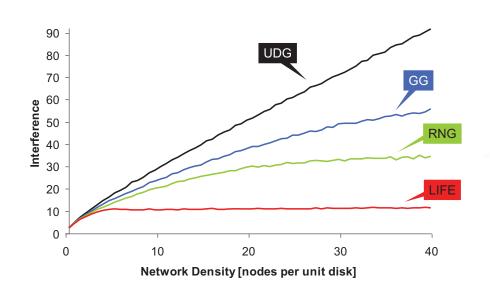
#### LIFE

- Attribute interference values as weights to edges
- Compute minimum spanning tree/forest (Kruskal's algorithm)





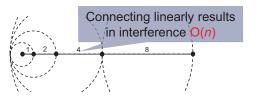
## Average-Case Interference: Preserve Connectivity



#### Node-based Interference Model



 Already 1-dimensional node distributions seem to yield inherently high interference...



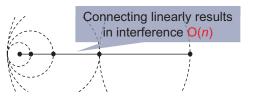
...but the exponential node chain can be connected in a better way

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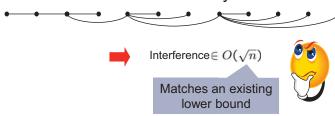
#### Node-based Interference Model



 Already 1-dimensional node distributions seem to yield inherently high interference...



...but the exponential node chain can be connected in a better way



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#### Node-based Interference Model



- · Arbitrary distributed nodes in one dimension
  - Approximation algorithm with approximation ratio in  $O(\sqrt[4]{n})$



- Two-dimensional node distributions
  - Simple randomized algorithm resulting in interference  $O(\sqrt{n \log n})$
  - Can be improved to  $O(\sqrt{n})$

# Open problem

- On the theory side there are quite a few open problems. Even the simplest questions of the node-based interference model are open:
- We are given n nodes (points) in the plane, in arbitrary (worst-case) position. You must connect the nodes by a spanning tree. The neighbors of a node are the direct neighbors in the spanning tree. Now draw a circle around each node, centered at the node, with the radius being the minimal radius such that all the nodes' neighbors are included in the circle. The interference of a node u is defined as the number of circles that include the node u. The interference of the graph is the maximum node interference. We are interested to construct the spanning tree in a way that minimizes the interference. Many questions are open: Is this problem in P, or is it NP-complete? Is there a good approximation algorithm? Etc.