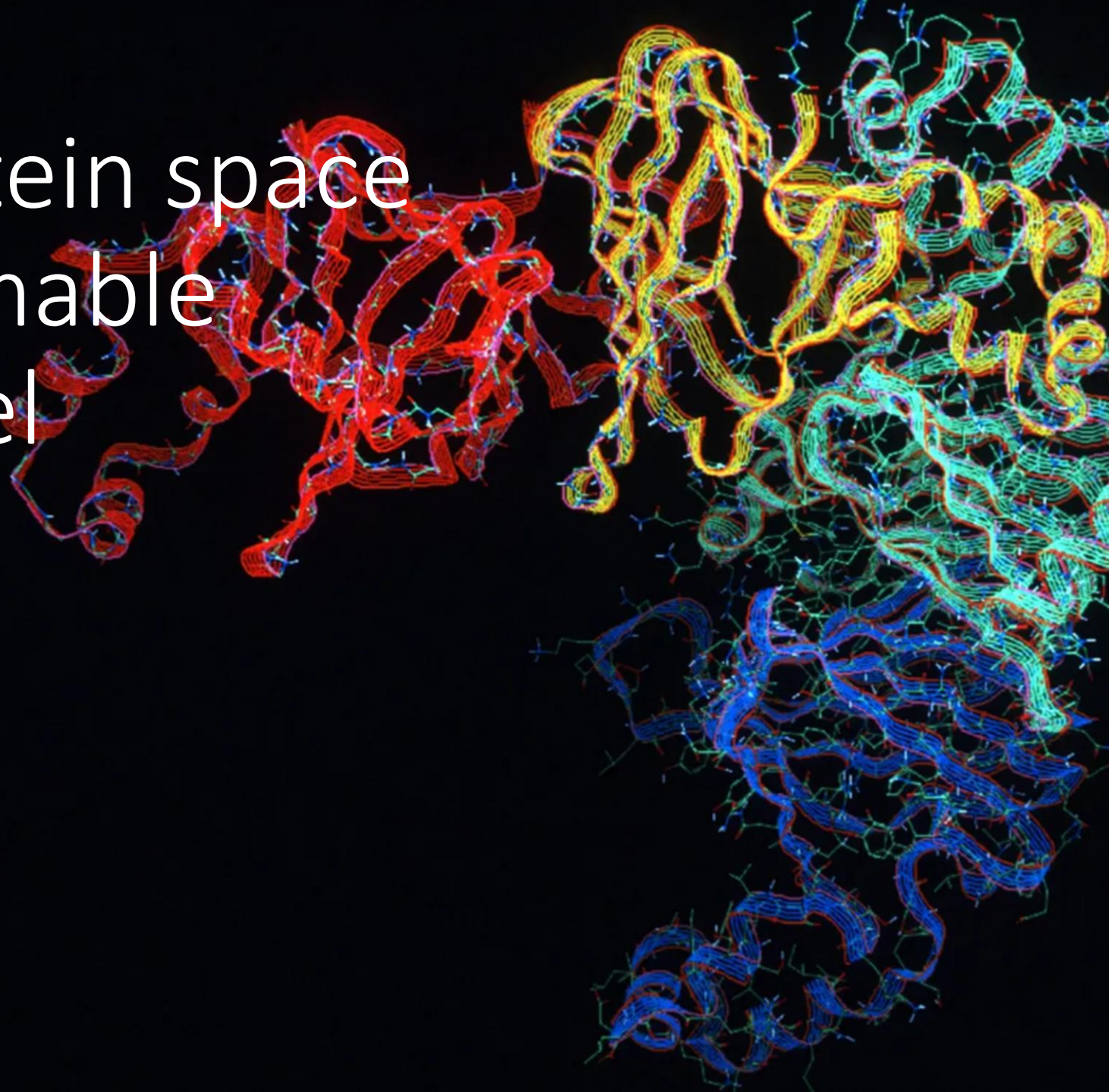


Illuminating protein space with a programmable generative model

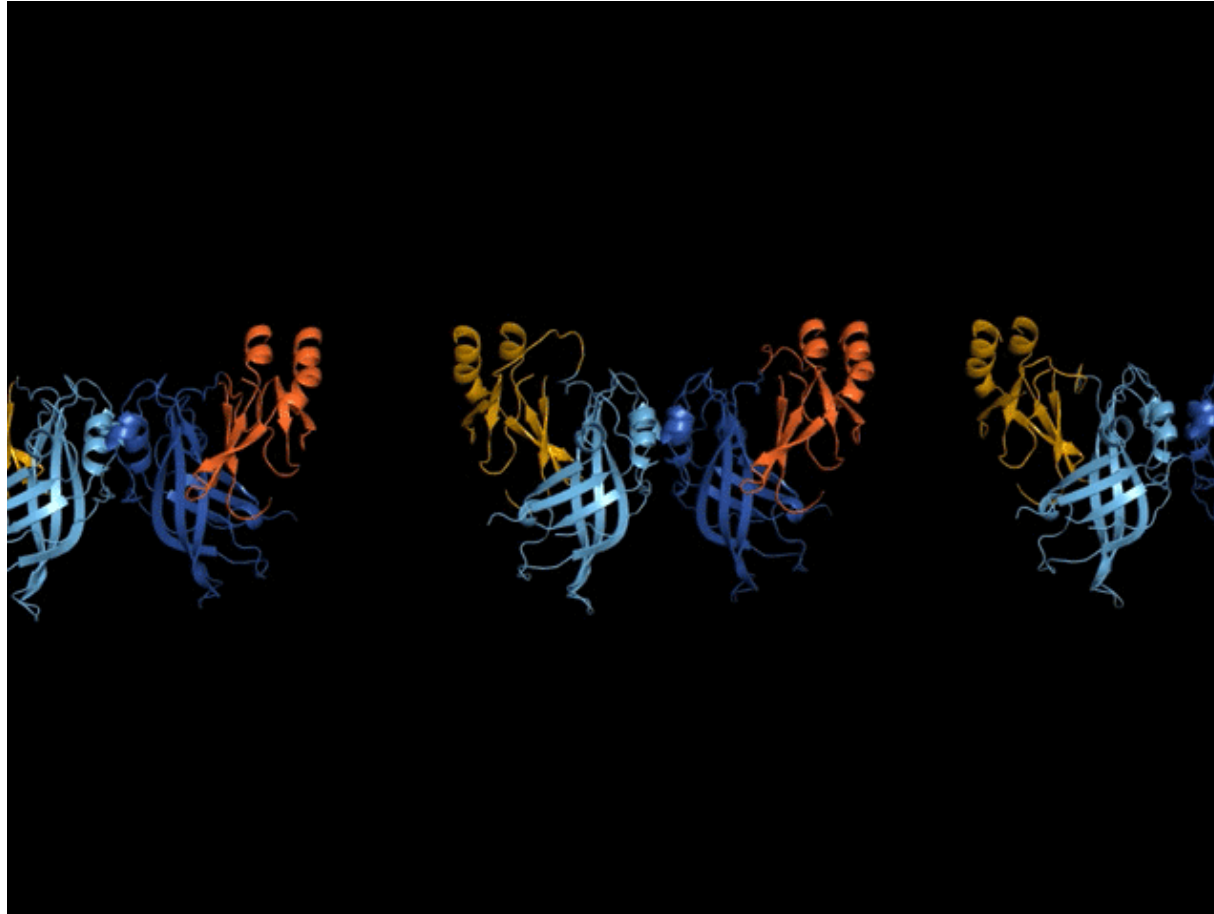
J Ingraham, M Baranov, Z Costello, V Frappier,
A Ismail, S Tie, W Wang, V Xue, F Obermeyer,
A Beam, G Grigoryan

December 1, 2022

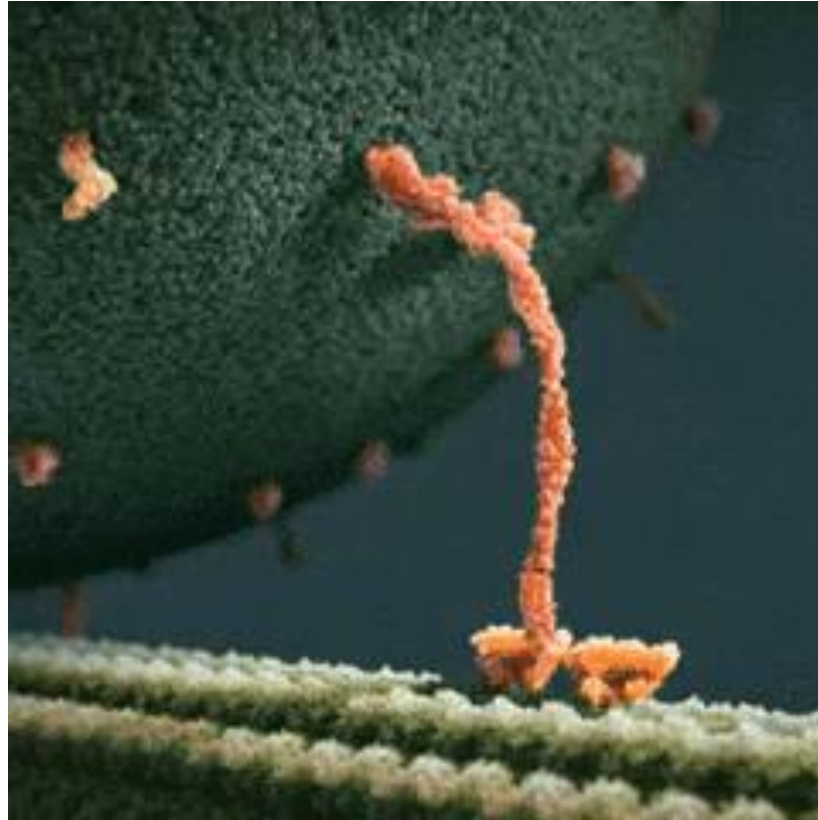
Presented by Meret Ackermann



Proteins – the chief actors in cells



Structure – the key component of function

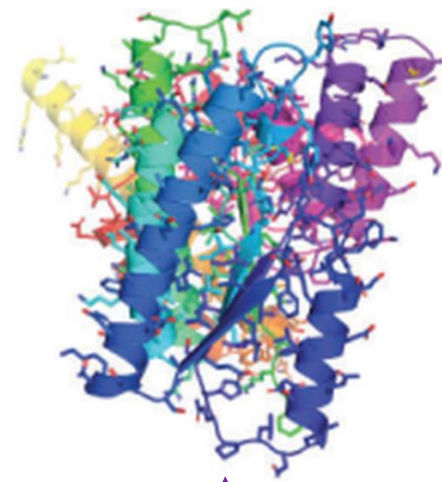


Protein Structure Prediction

Sequence

V	N	E	C	I	K	N	A	P	A	.	A	G	S	T	S	L	L
A	E	N	A	I	Q	Q	M	G	G	.	Q	W	L	G	G	R	Q
A	A	M	A	I	R	A	L	N	G	.	Y	T	M	G	N	R	V
A	E	K	A	M	E	E	L	N	Y	.	T	K	V	N	G	K	E
M	I	R	A	I	D	T	F	N	G	.	M	E	V	E	G	R	V
A	D	K	A	V	E	L	Y	S	Q	.	Y	D	L	N	G	R	L
A	K	D	A	A	R	D	M	N	G	.	K	S	L	D	G	K	A
A	E	A	A	V	Q	A	L	N	G	K	D	M	G	E	G	K	S
M	K	D	A	I	D	E	M	N	G	.	K	E	L	D	G	R	T
A	E	K	A	I	N	T	L	N	G	.	L	R	L	Q	T	K	T
T	K	E	A	L	A	K	A	R	K	.	T	K	F	N	G	H	I
L	L	S	A	L	S	.	L	N	E	.	E	S	L	G	N	R	R
V	Q	D	A	I	S	K	F	D	G	.	A	L	F	M	D	R	K
A	K	K	A	L	D	A	L	Q	G	.	E	Y	I	D	N	R	P
A	A	V	C	I	V	A	L	A	N	.	F	P	F	Q	G	R	N

Folding

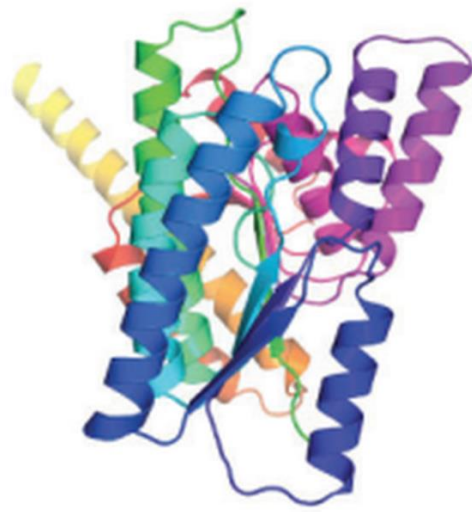


AlphaFold
RosettaFold

...

Protein Sequence prediction

Structure



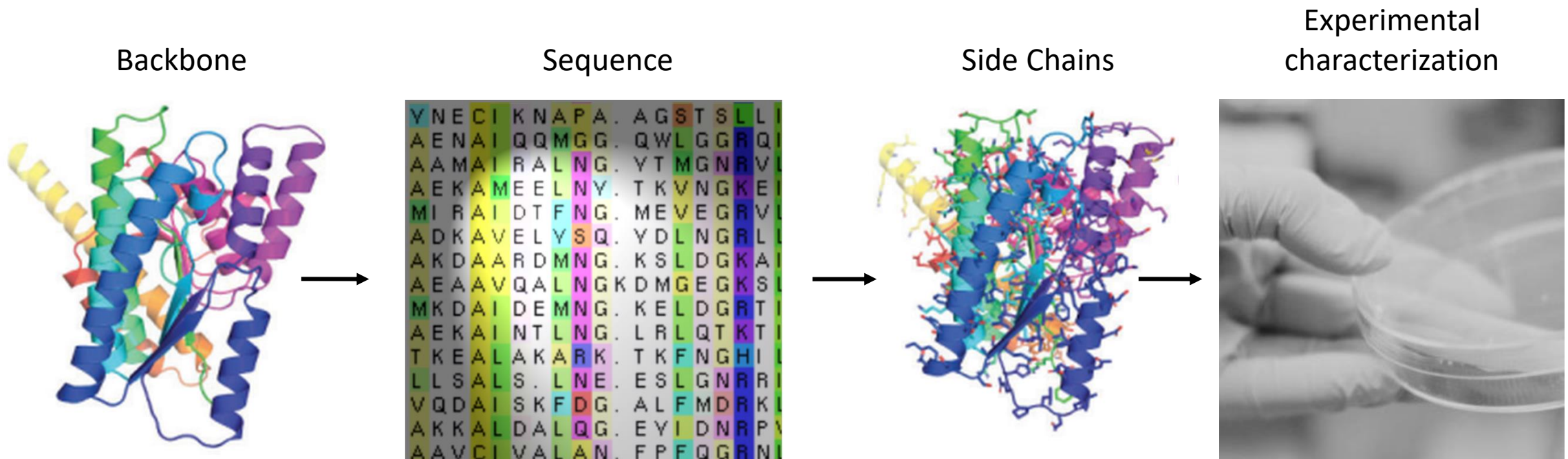
↓
Protein MPNN
GVP-GNN
...

Folding

V	N	E	C	I	K	N	A	P	A	.	A	G	S	T	S	L	L	I
A	E	N	A	I	Q	Q	M	G	G	.	Q	W	L	G	G	R	Q	I
A	A	M	A	I	R	A	L	N	G	.	Y	T	M	G	N	R	V	I
A	E	K	A	M	E	E	L	N	Y	.	T	K	V	N	G	K	E	I
M	I	R	A	I	D	T	F	N	G	.	M	E	V	E	G	R	V	I
A	D	K	A	V	E	L	Y	S	Q	.	Y	D	L	N	G	R	L	I
A	K	D	A	A	R	D	M	N	G	.	K	S	L	D	G	K	A	I
A	E	A	A	V	Q	A	L	N	G	K	D	M	G	E	G	K	S	I
M	K	D	A	I	D	E	M	N	G	.	K	E	L	D	G	R	T	I
A	E	K	A	I	N	T	L	N	G	.	L	R	L	Q	T	K	T	I
T	K	E	A	L	A	K	A	R	K	.	T	K	F	N	G	H	I	I
L	L	S	A	L	S	.	L	N	E	.	E	S	L	G	N	R	R	I
V	Q	D	A	I	S	K	F	D	G	.	A	L	F	M	D	R	K	I
A	K	K	A	L	D	A	L	Q	G	.	E	Y	I	D	N	R	P	I
A	A	V	C	I	V	A	L	A	N	.	F	P	F	Q	G	R	N	I



Structure first – Protein Design



Generative diffusion process

Forward SDE. **Training.** Data to Noise.

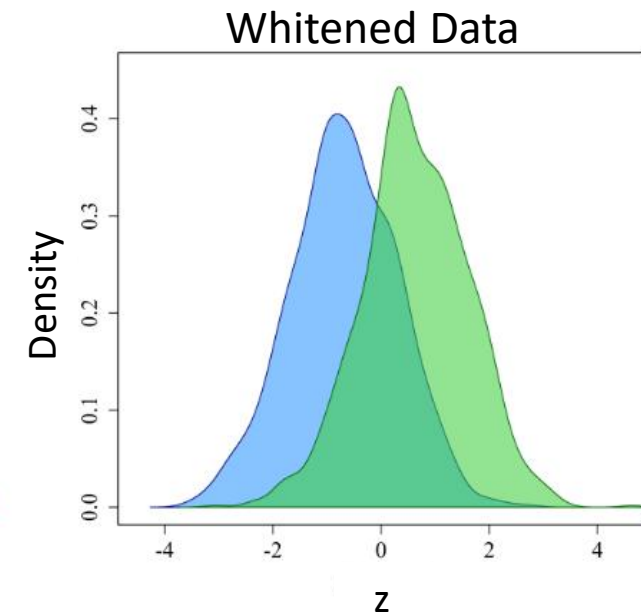
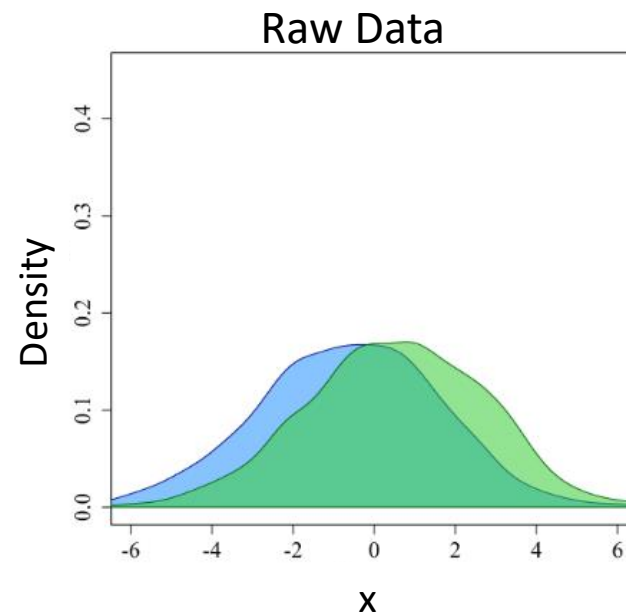
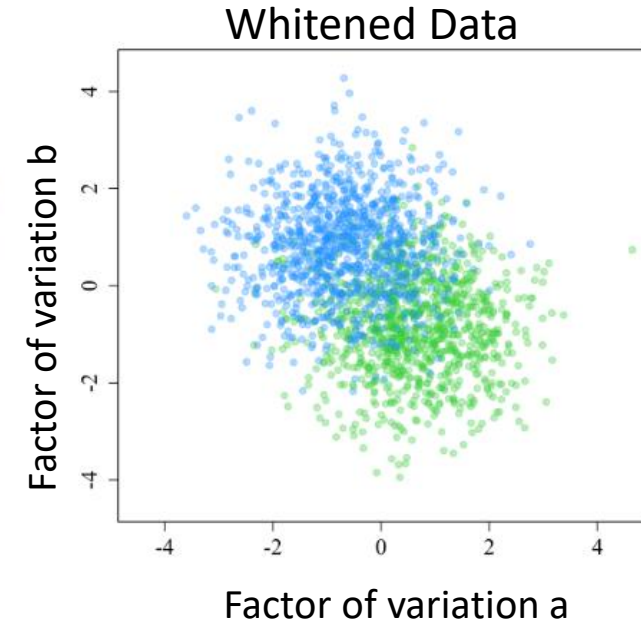
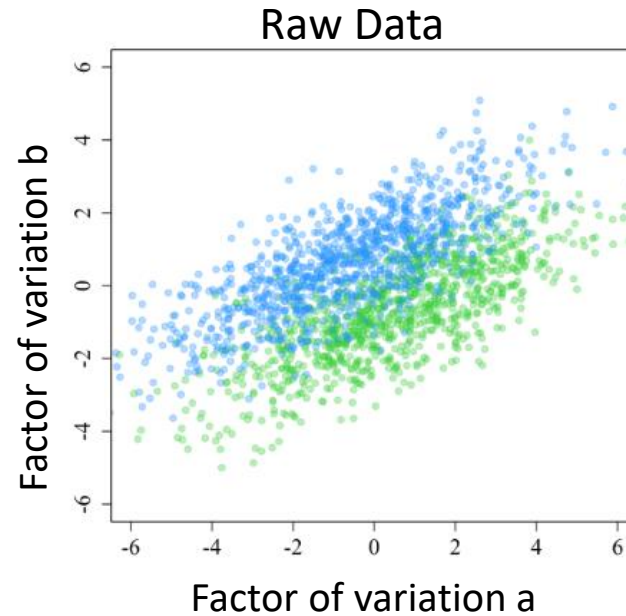


Reverse SDE. **Generation.** Noise to Data

Whitening transformation

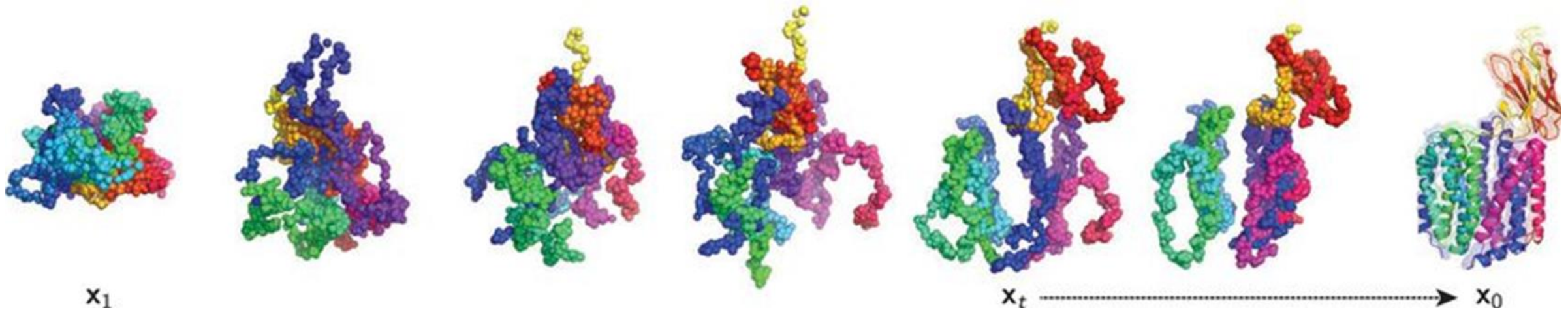
Correlated diffusion
as uncorrelated diffusion
in whitened space

$$\mathbf{z} = \mathbf{R}(\mathbf{x} - \boldsymbol{\mu})$$

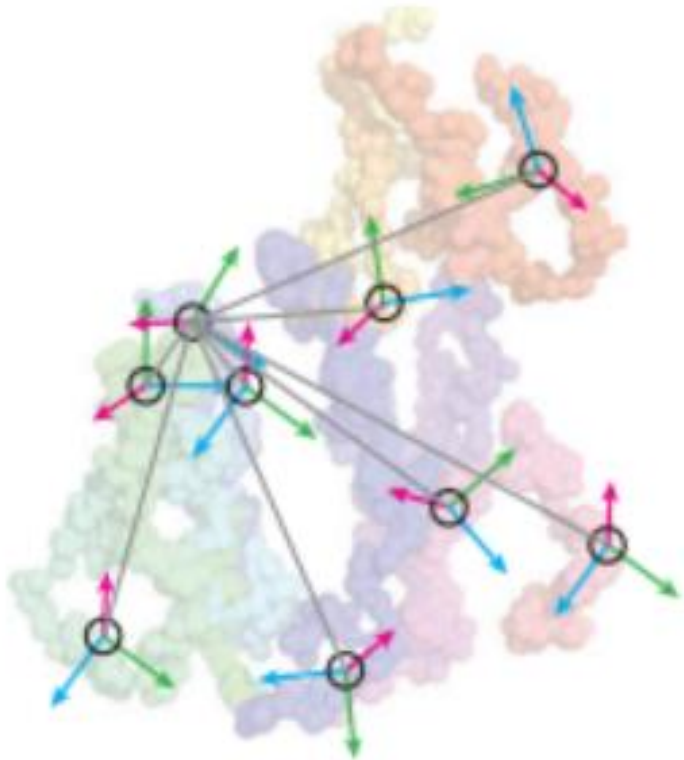


Correlated forward SDE process

$$dx = Rdz = -\frac{\beta_t}{2}Rzdt + \sqrt{\beta_t}Rdw$$

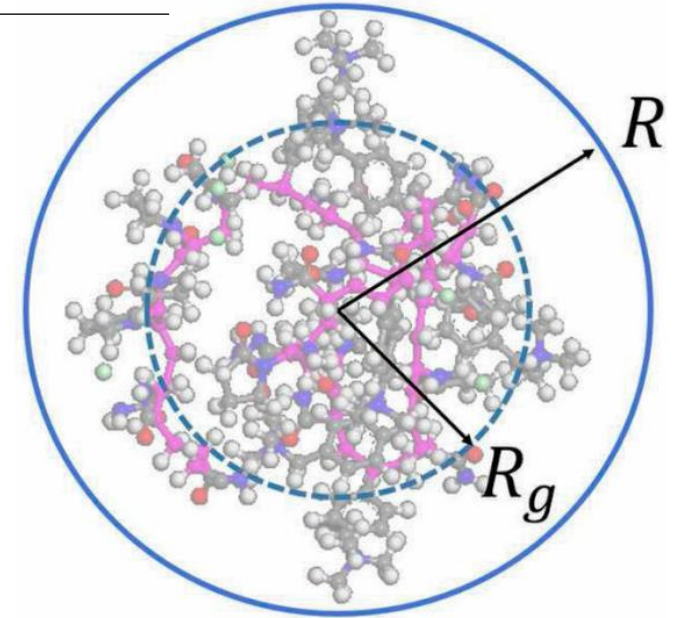


Constraints as a de-whitening transform

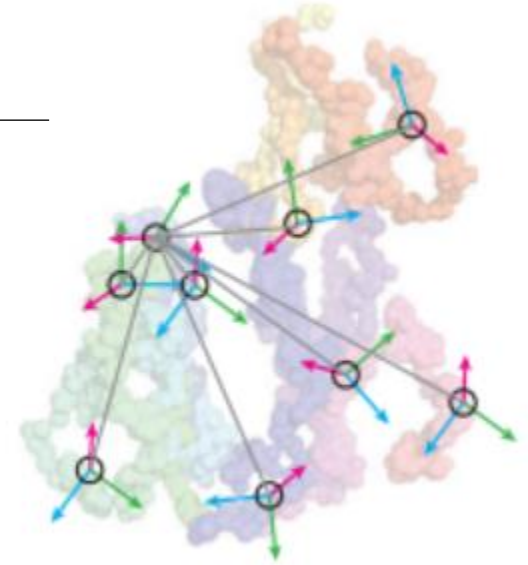
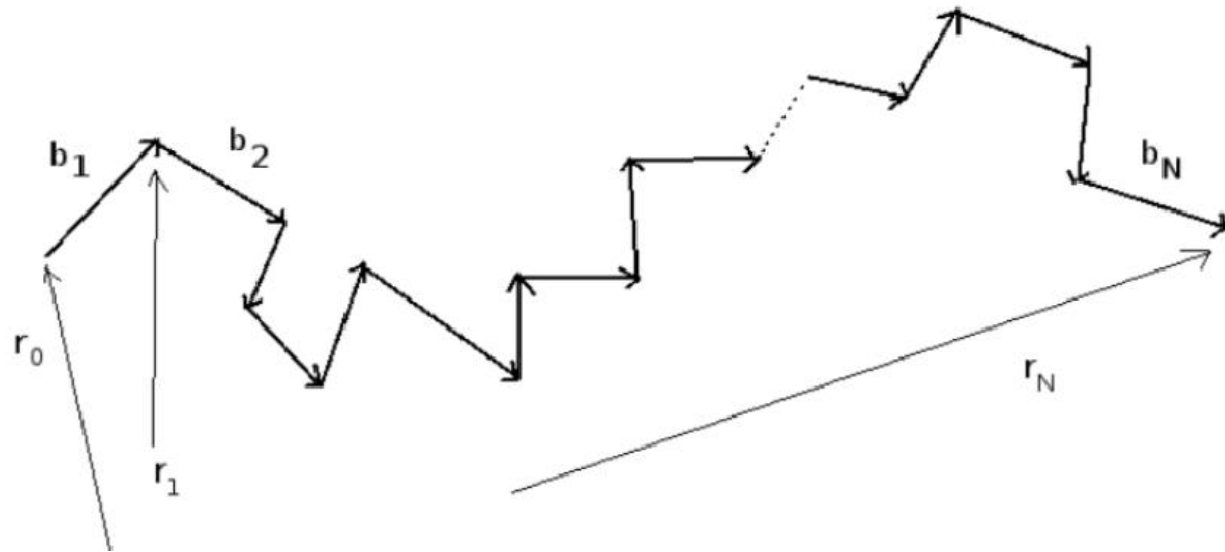


$$F(\mathbf{x}) = \sum_{i,j} A_{i,j} \mathbf{x}_i \mathbf{x}_j$$

$$\mathbb{E}_{p(\mathbf{x}_t|\mathbf{x}_0)}[F(\mathbf{x})] = \alpha_t F(\mathbf{x}_0) + (1 - \alpha_t) \mathbb{E}_{p_{model}(\mathbf{x})}[F(\mathbf{x})]$$



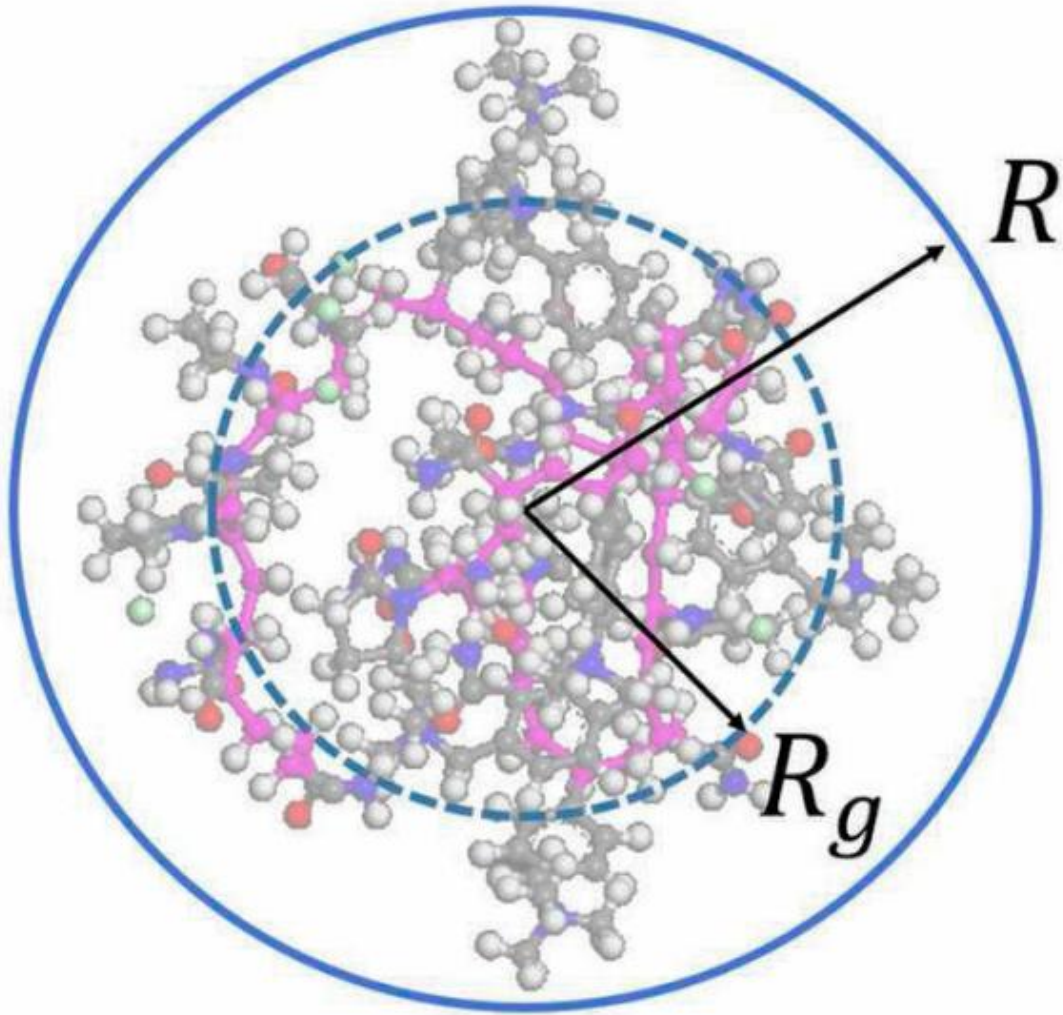
Constraint – Chain Structure



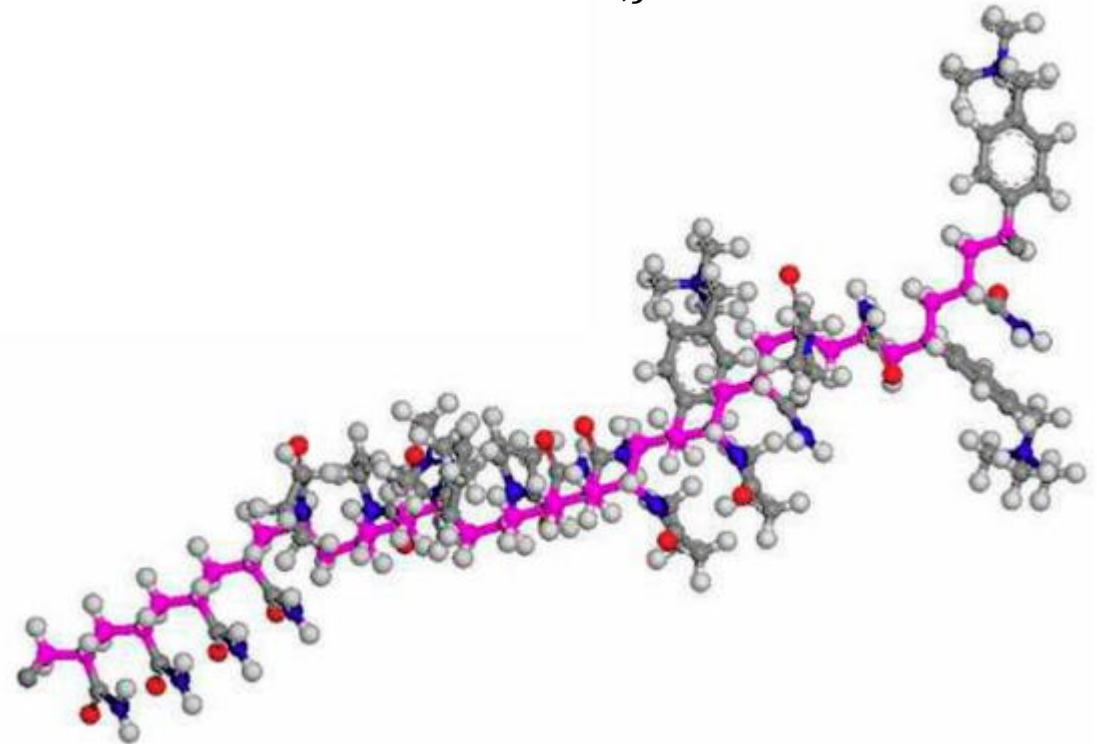
$$\mathbf{r}_{i,j} \sim \mathcal{N}(0, \gamma^2 |i - j|)$$

$$\mathbb{E}_{p(\mathbf{x}_t | \mathbf{x}_0)} [D_{ij}^2(\mathbf{x}_t)] = \alpha_t D_{ij}^2(\mathbf{x}_0) + (1 - \alpha_t) 3\gamma^2 |i - j|$$

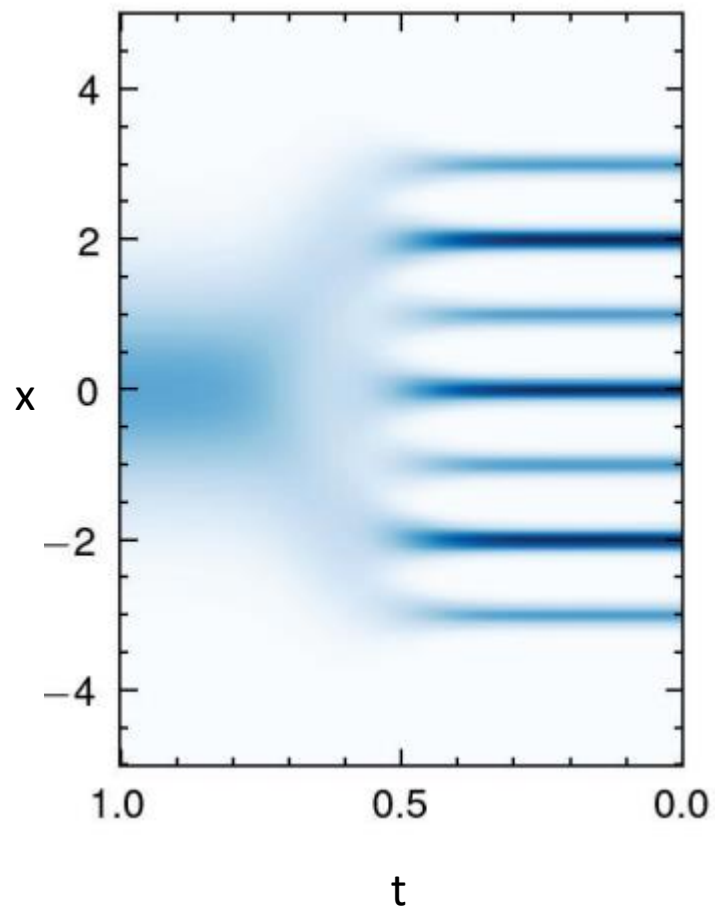
Constraint - Radius of Gyration



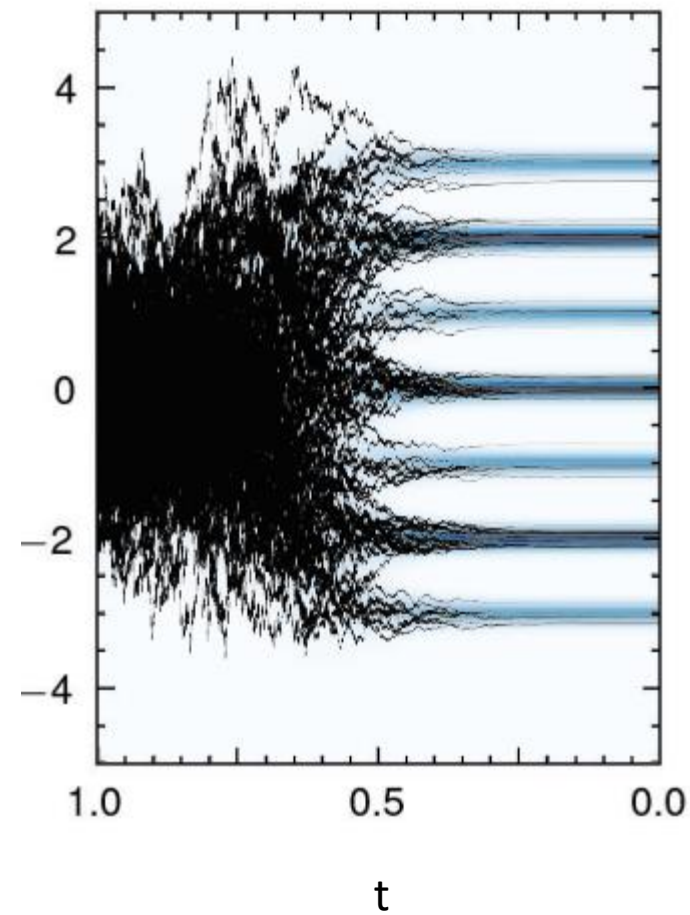
$$R_g^2(x) = \frac{1}{2N^2} \sum_{i,j} D_{i,j}^2(x)$$



Reverse-time SDE



$$dx = \left(-\frac{1}{2} \mathbf{x} - \mathbf{R}\mathbf{R}^T \nabla_x \log \mathbf{p}_t(\mathbf{x}) \right) \beta_t dt + \sqrt{\beta_t} \mathbf{R} d\tilde{w}$$

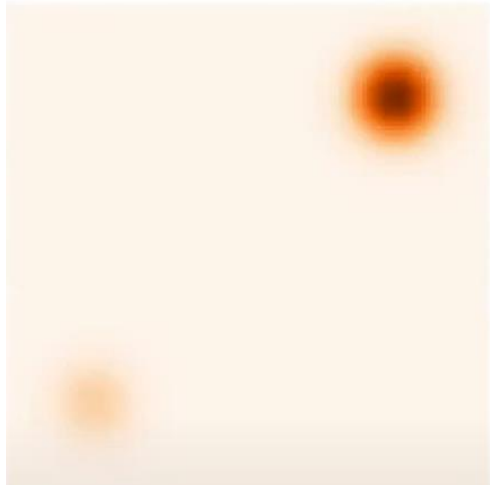


Correlated Reverse-time SDE



$$d\mathbf{x} = \left(-\frac{1}{2} \mathbf{x} - \mathbf{R}\mathbf{R}^T \nabla_{\mathbf{x}} \log \mathbf{p}_t(\mathbf{x}) \right) \beta_t dt + \sqrt{\beta_t} \mathbf{R} d\tilde{\mathbf{w}}$$

Score Estimation

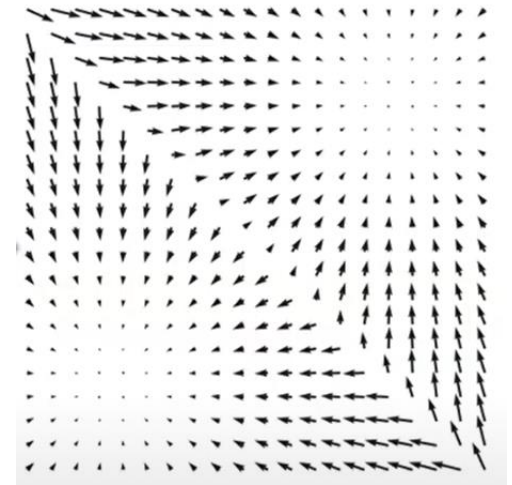


$$p_{data}(x)$$

$$\nabla_x \log p_{data}(x)$$



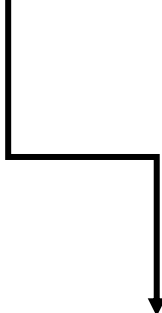
Samples



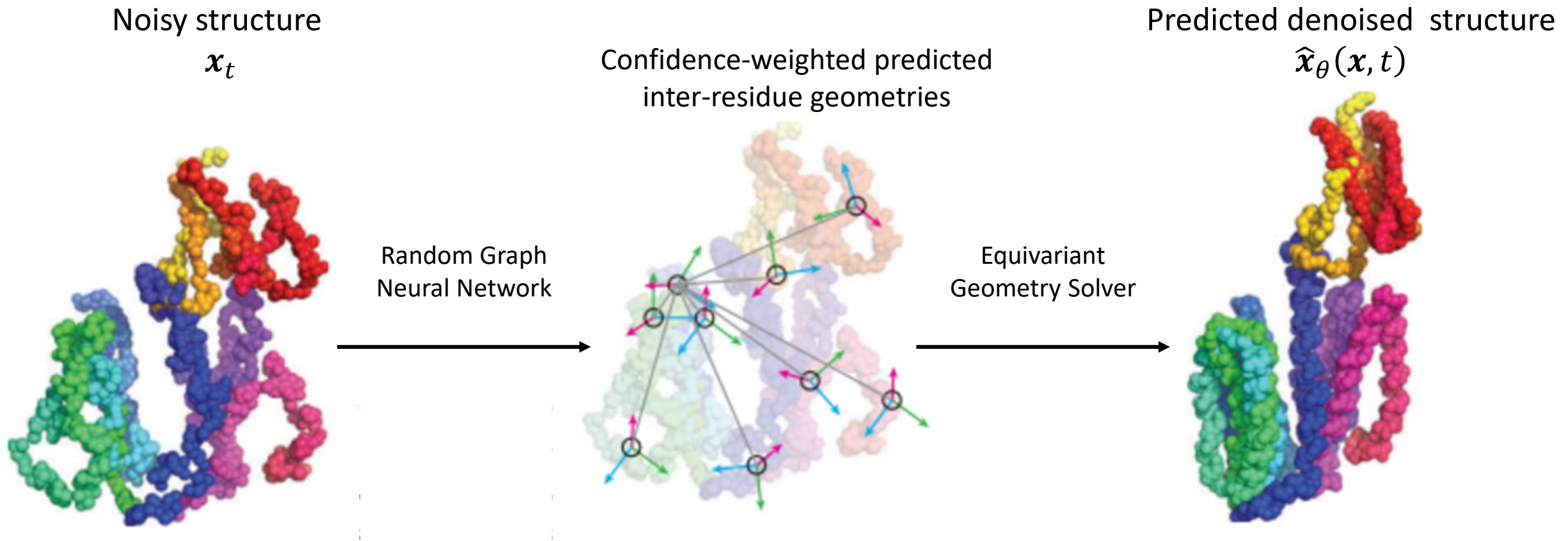
$$\sim \nabla_x \log p(x)$$

Optimized denoiser

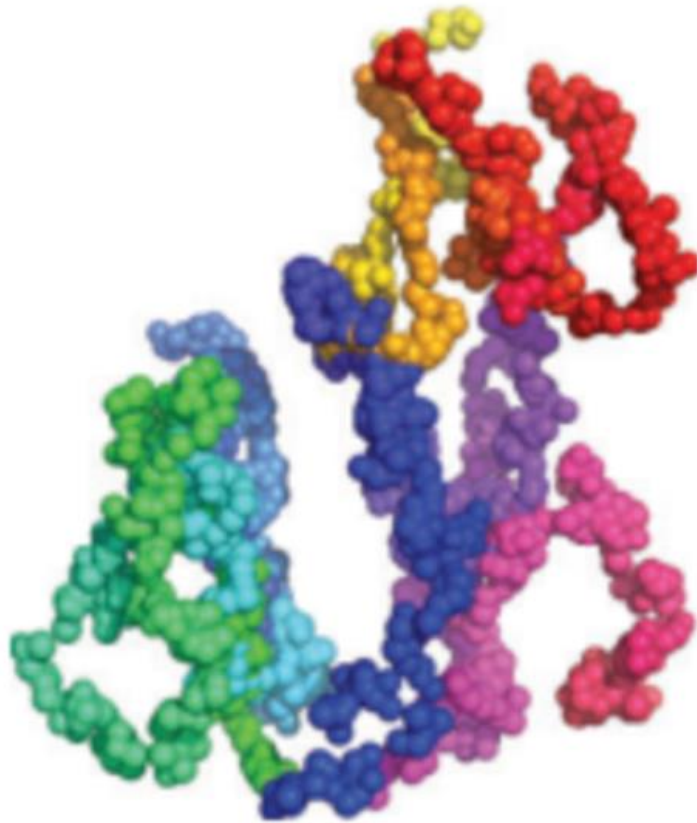
$$\nabla_{\mathbf{x}} \log p_t(\mathbf{x}) = \left((1 - \alpha_t) \mathbf{R} \mathbf{R}^T \right)^{-1} (\sqrt{\alpha_t} \hat{\mathbf{x}}_{\theta}(\mathbf{x}, t) - \mathbf{x})$$


$$\mathcal{L}_{\mathbf{x}}^{\text{reg}}(\mathbf{x}; \theta) = -\mathbb{E}_{\mathbf{x}_t \sim p(\mathbf{x}_t | \mathbf{x}), t \sim \text{Unif}(0,1)} \left[\frac{\alpha_t \beta_t}{2(1 - \alpha_t)^2} \left\| (\mathbf{R}^{-1} + \omega \mathbf{I}) (\hat{\mathbf{x}}_{\theta}(\mathbf{x}_t, t) - \mathbf{x}) \right\|_2^2 \right]$$

Optimized denoiser



Reduced computational complexity



Random Graph
Neural Network



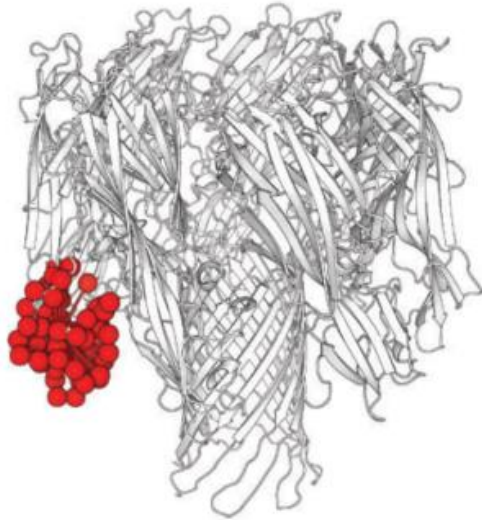
$\mathcal{O}(N \log N)$
or
 $\mathcal{O}(N)$
edges



Sub- $\mathcal{O}(N^2)$ scaling - Random edge sampling

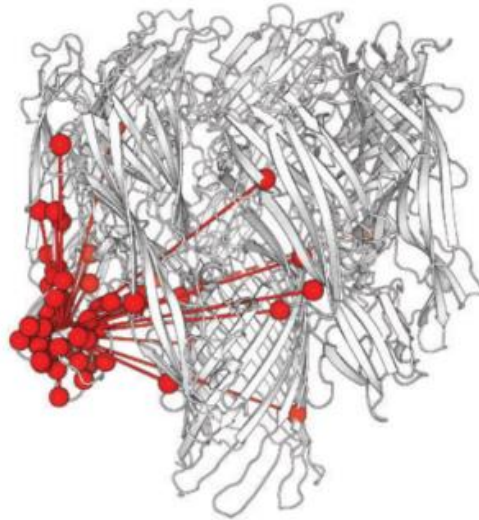
Deterministic graph

k -NN



Random graphs

Inverse cubic

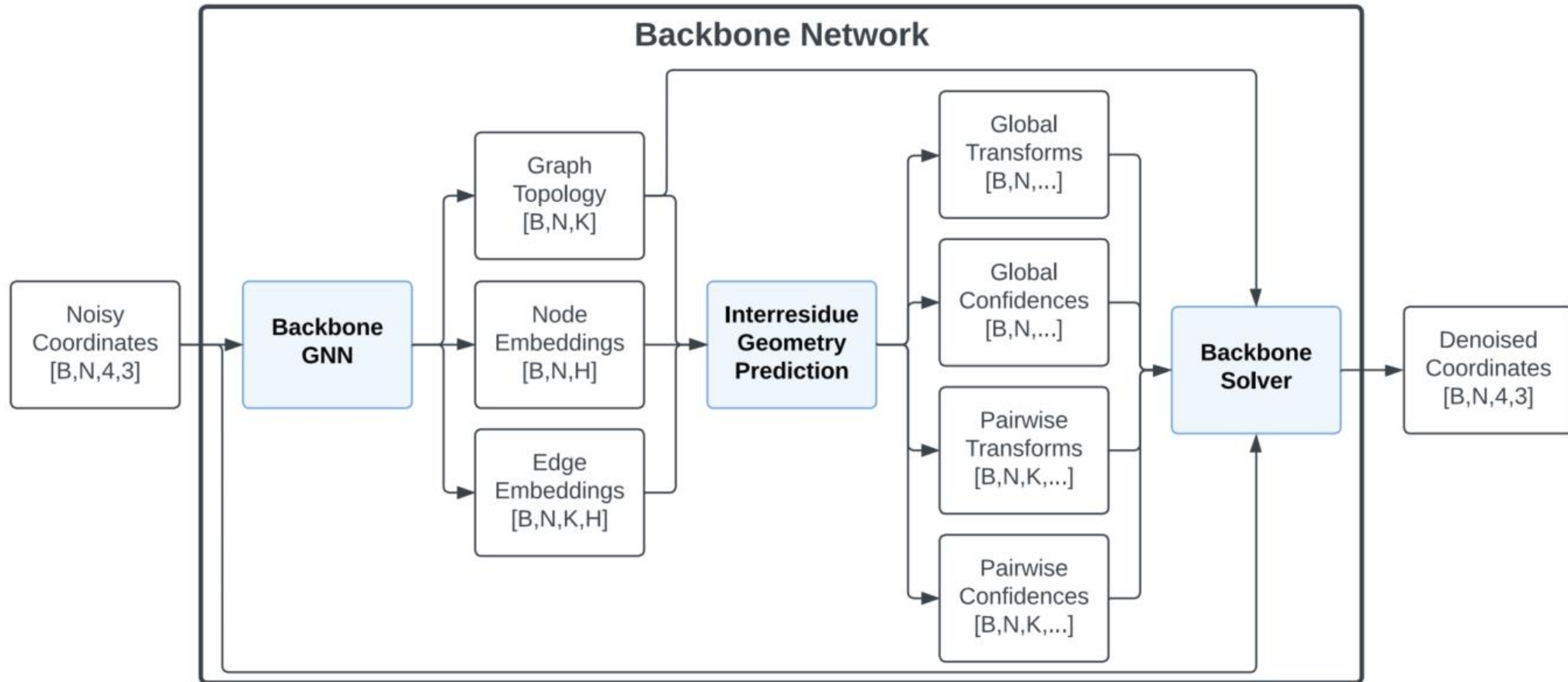


Mixed graph

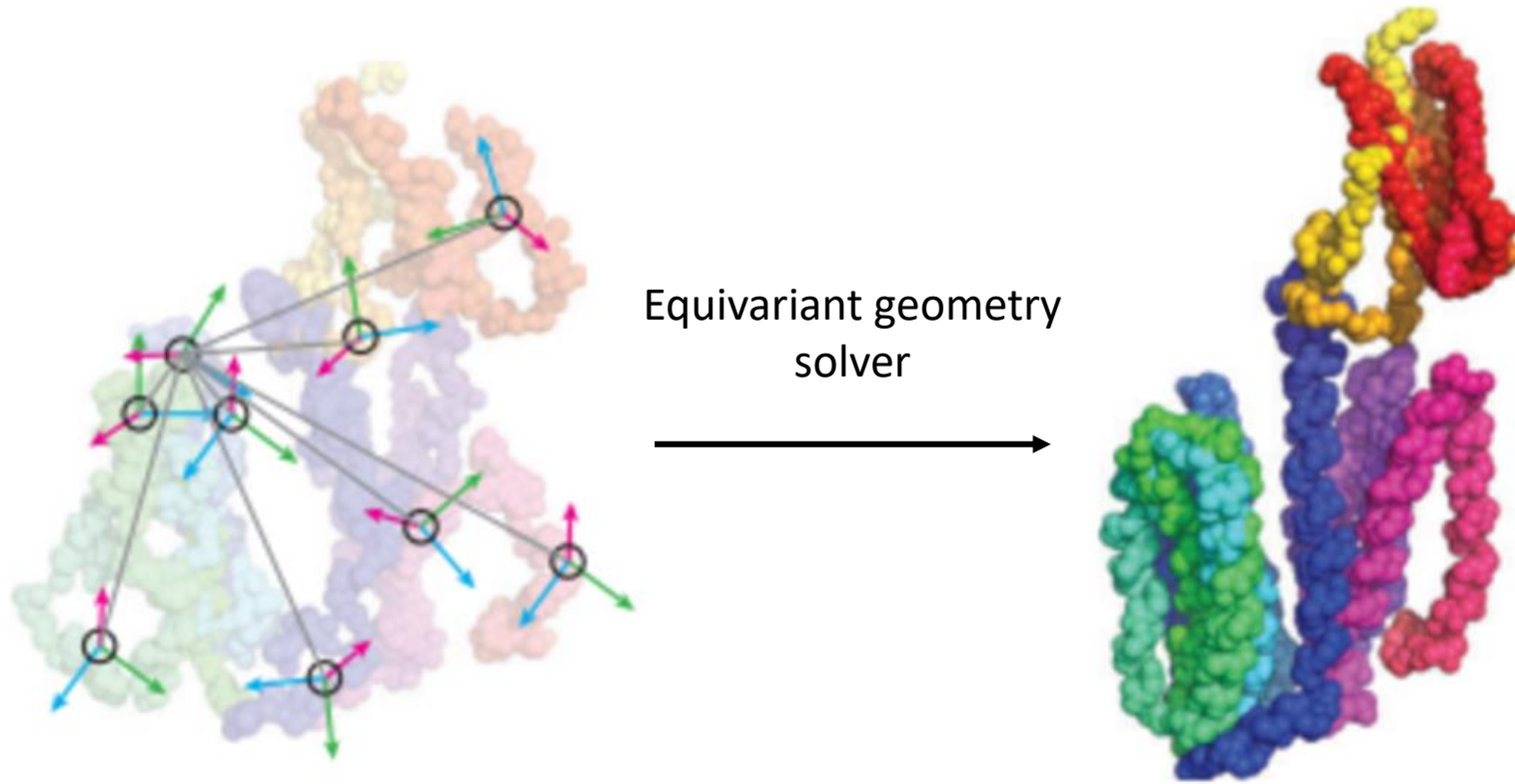
20 k -NN + 40 Inverse Cubic



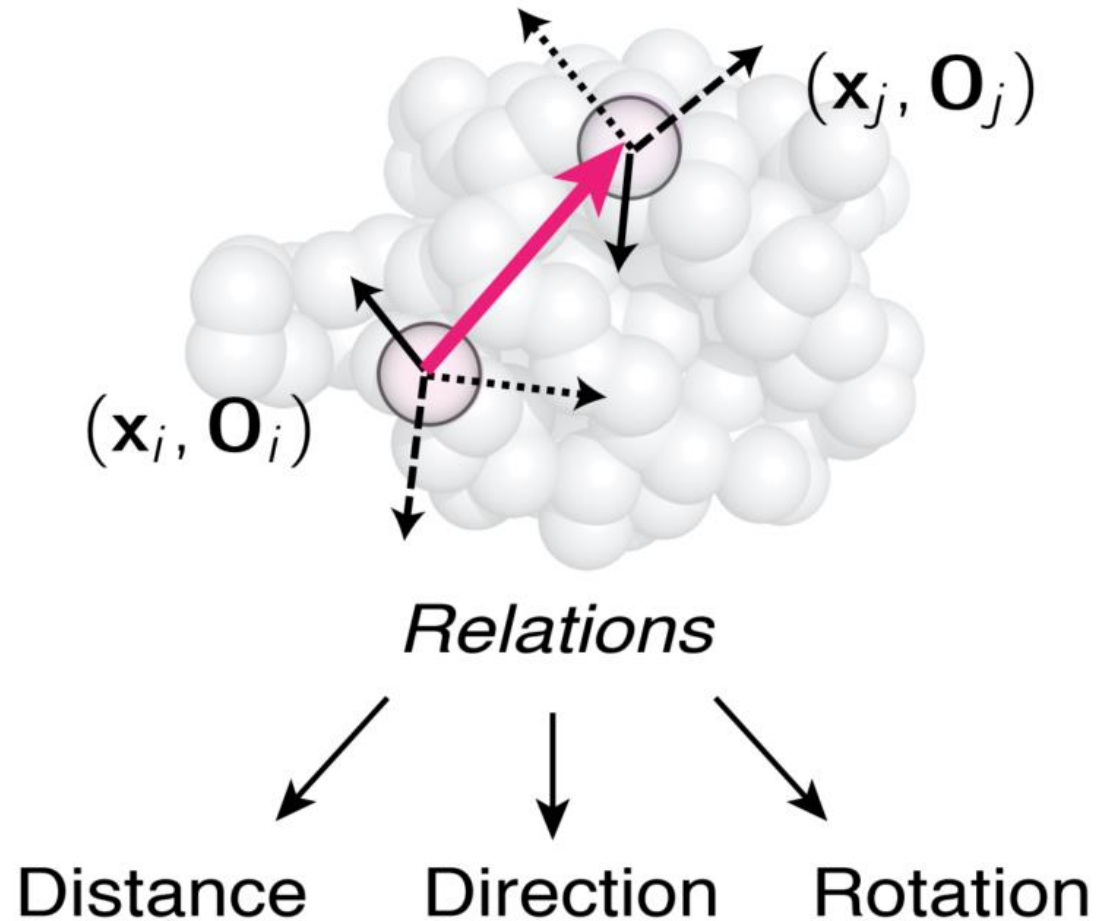
Backbone graph neural network



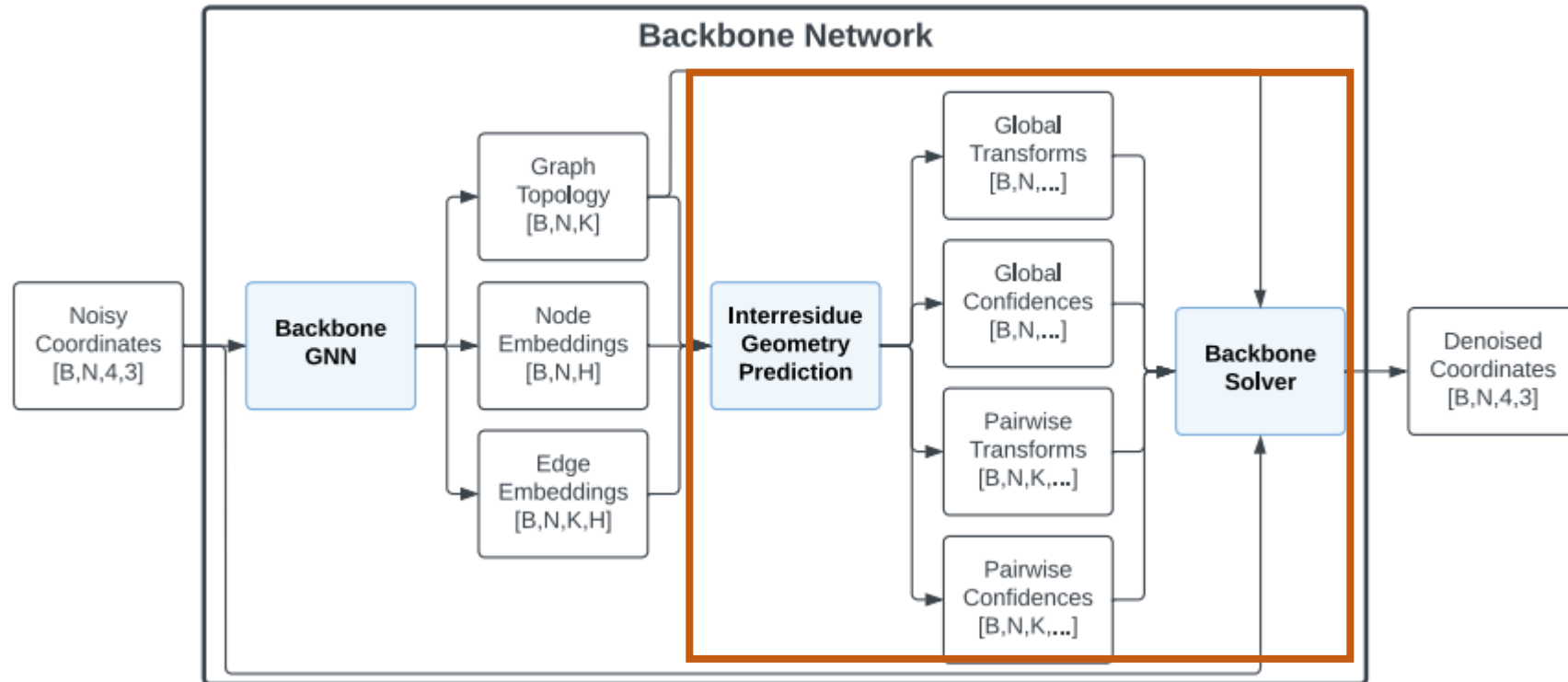
Equivariant geometry solver



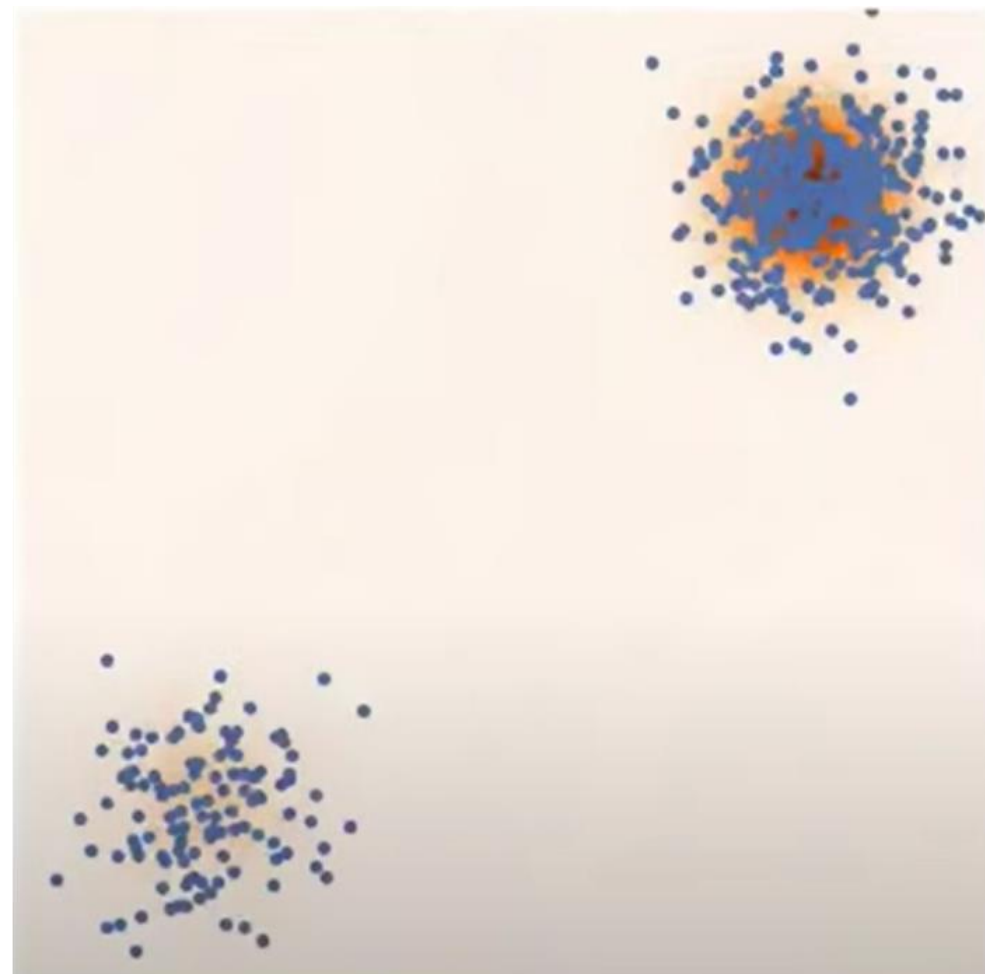
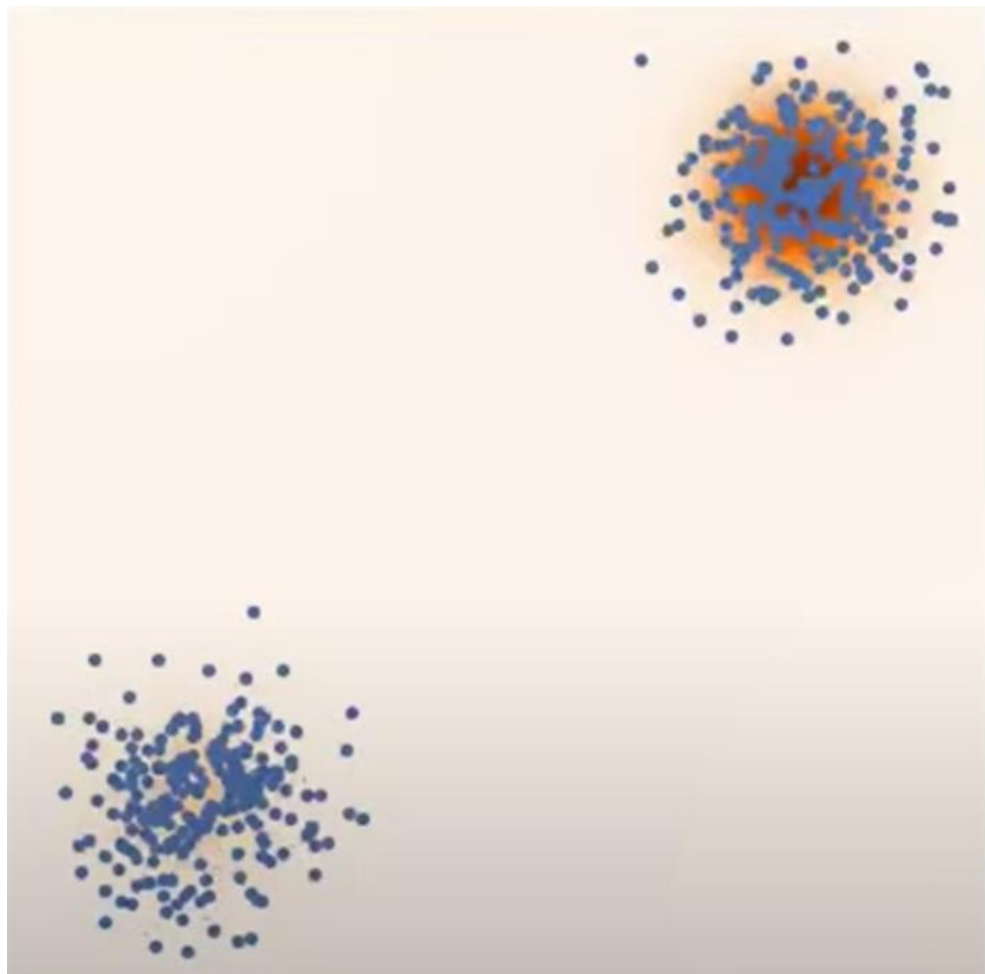
Invariant local frame relations



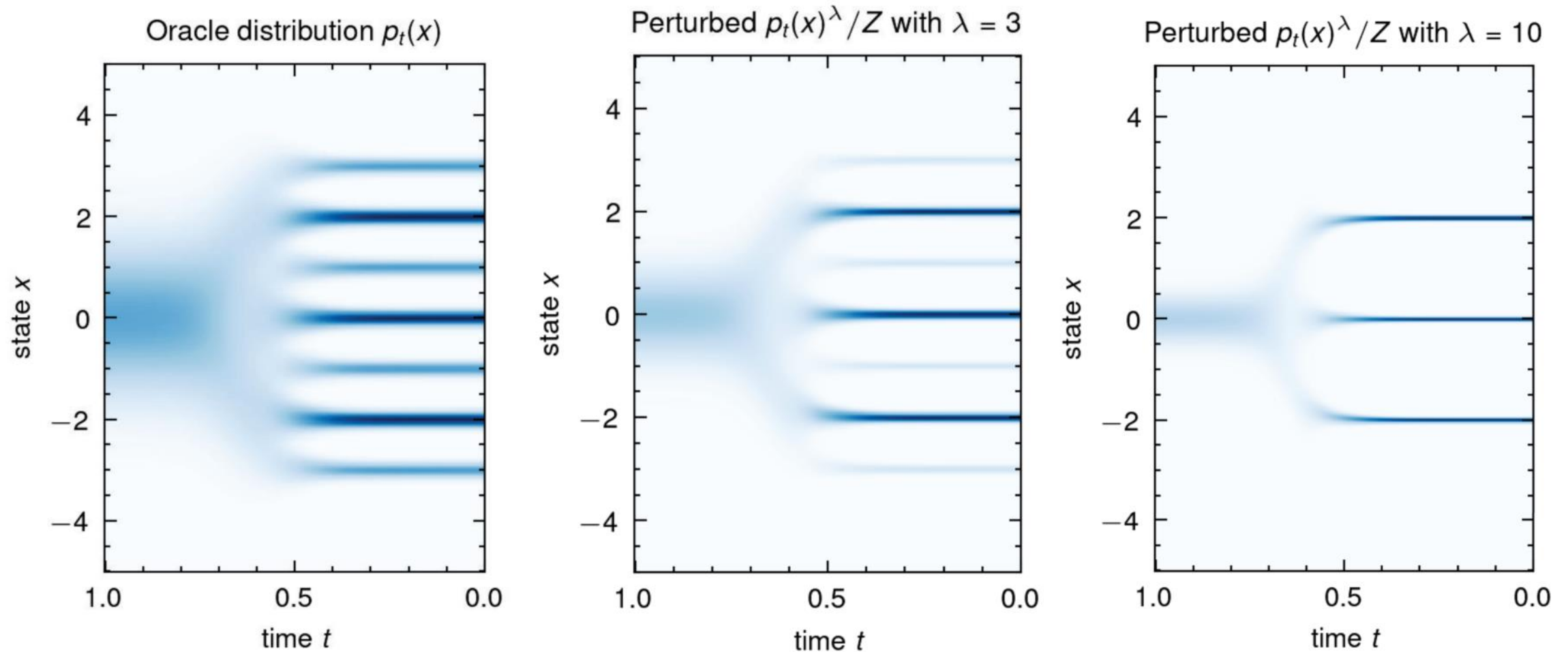
Equivariant geometry solver



Sampling of the backbone - overdispersion

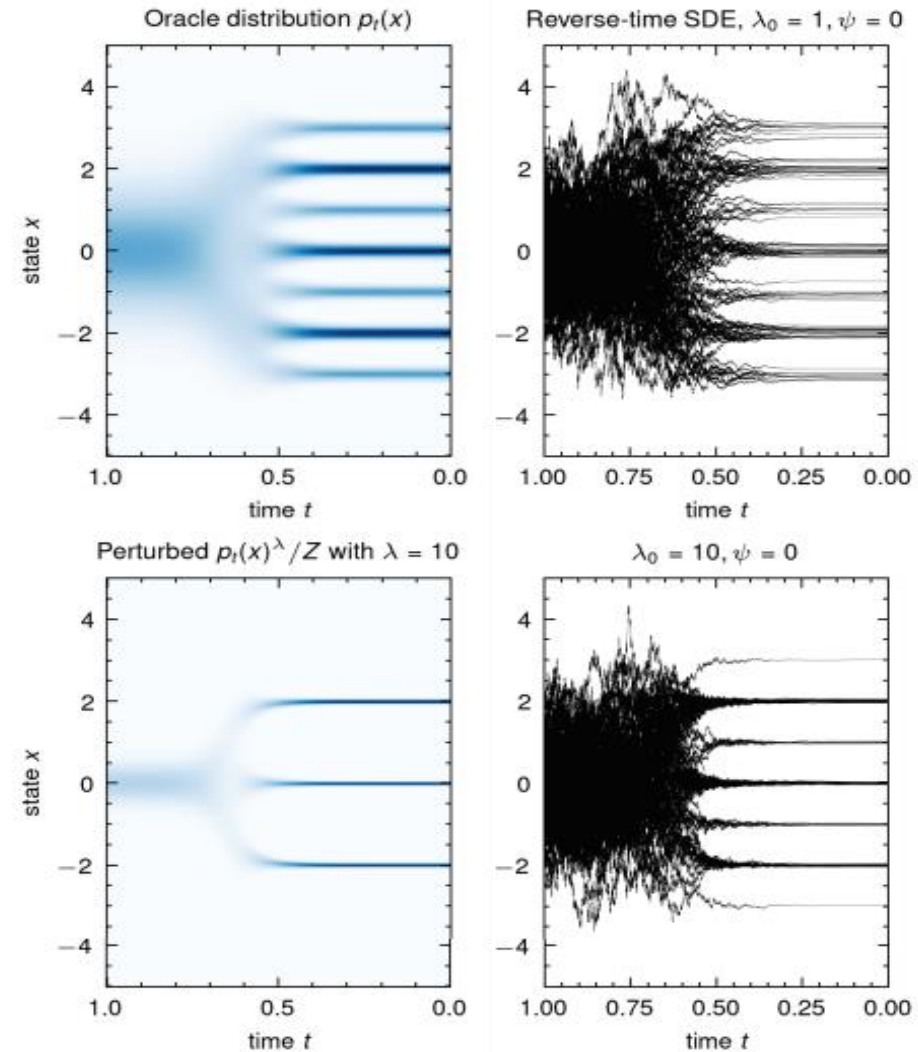


Low temperature sampling – reweight and concentrate



Annealed reverse-time SDE

$$\lambda_t \approx \frac{\lambda_0}{\alpha_t + (1 - \alpha_t)\lambda_0}$$

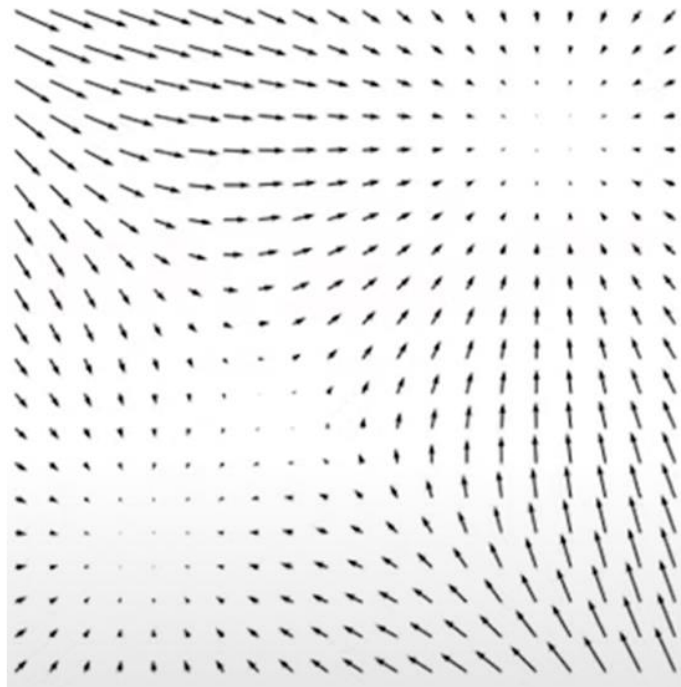


Score evolution

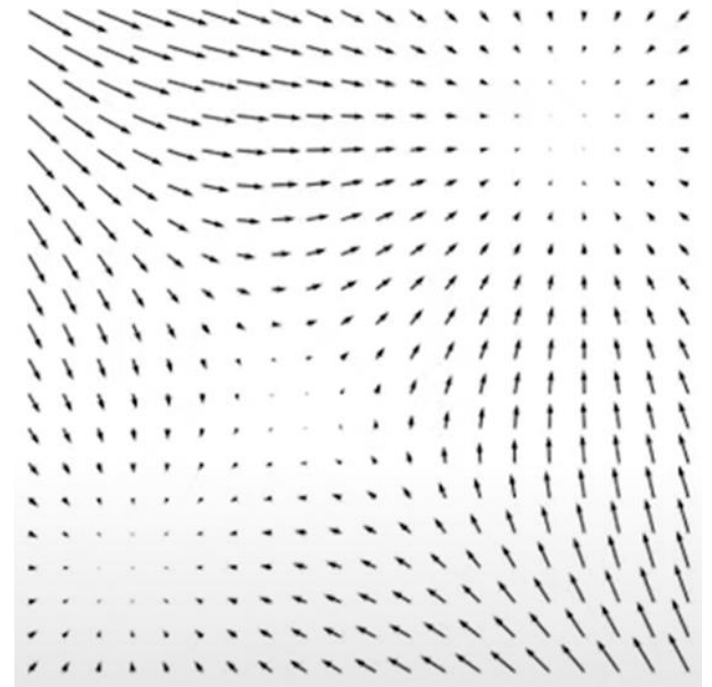
Data Density



Data Score

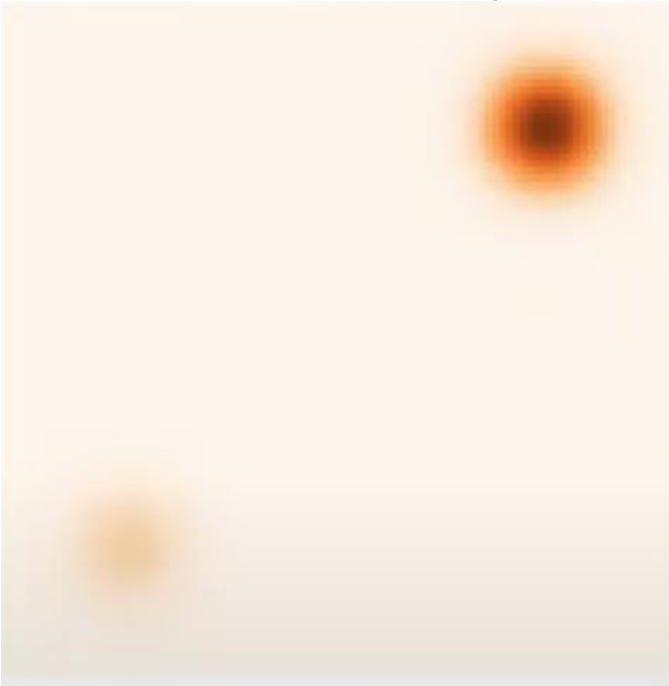


Estimated Score

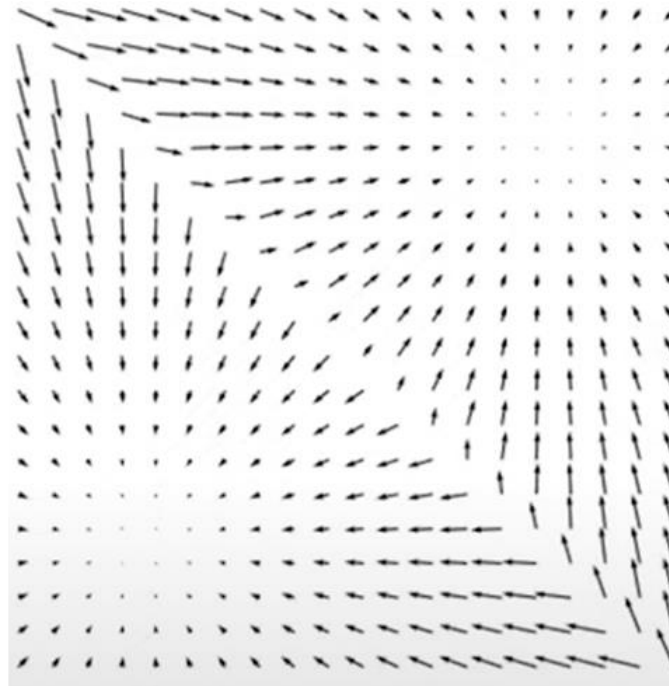


Score evolution

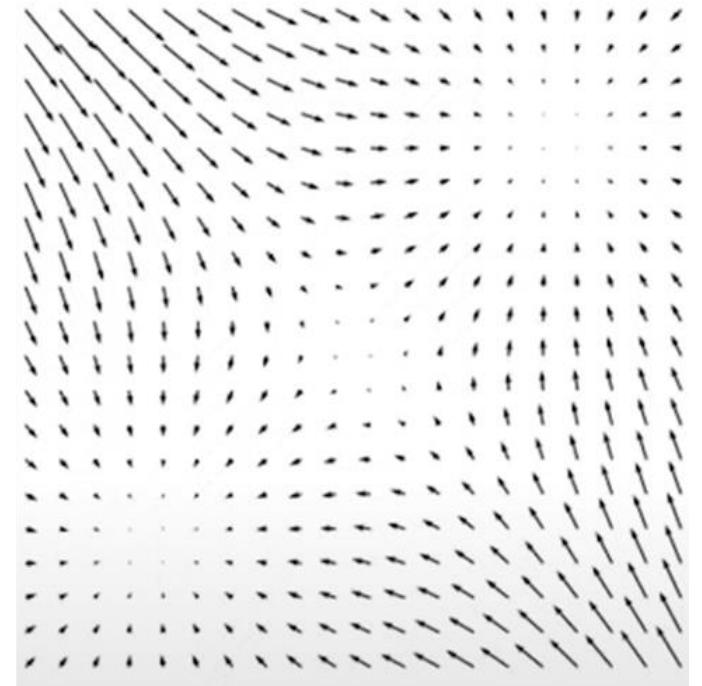
Data Density



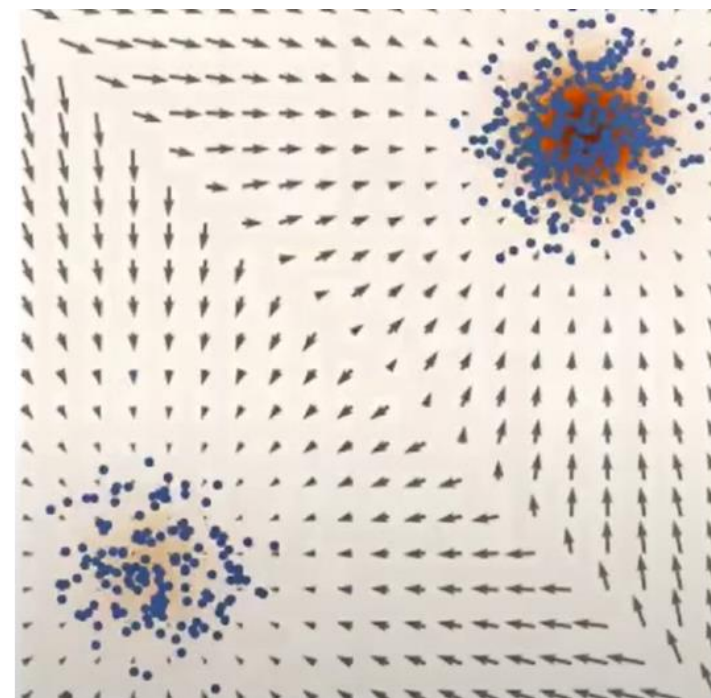
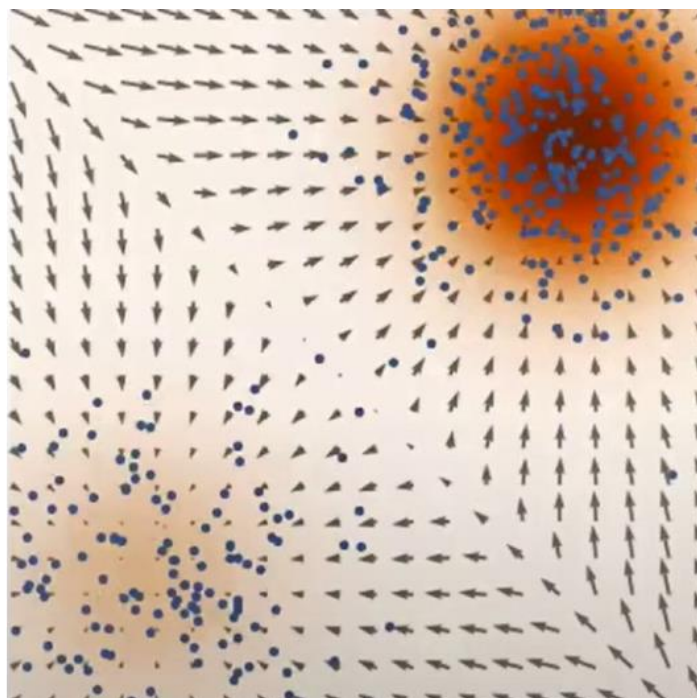
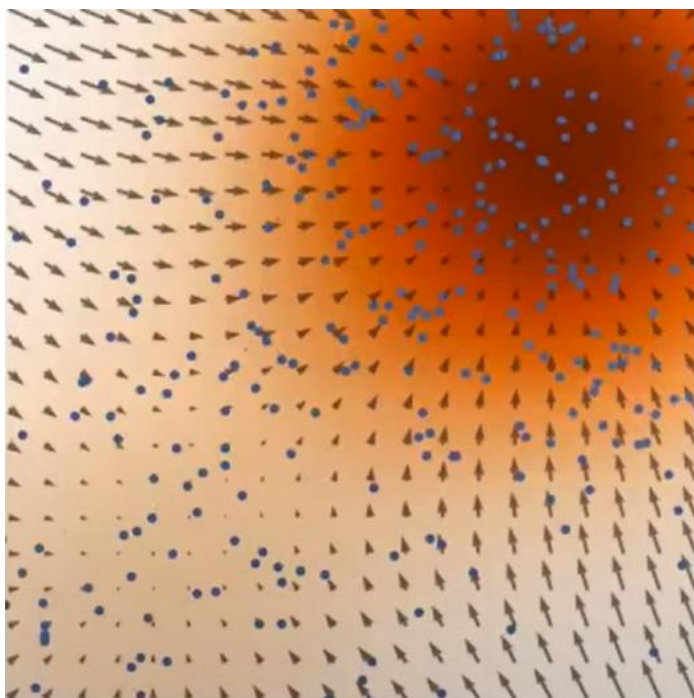
Data Score



Estimated Score

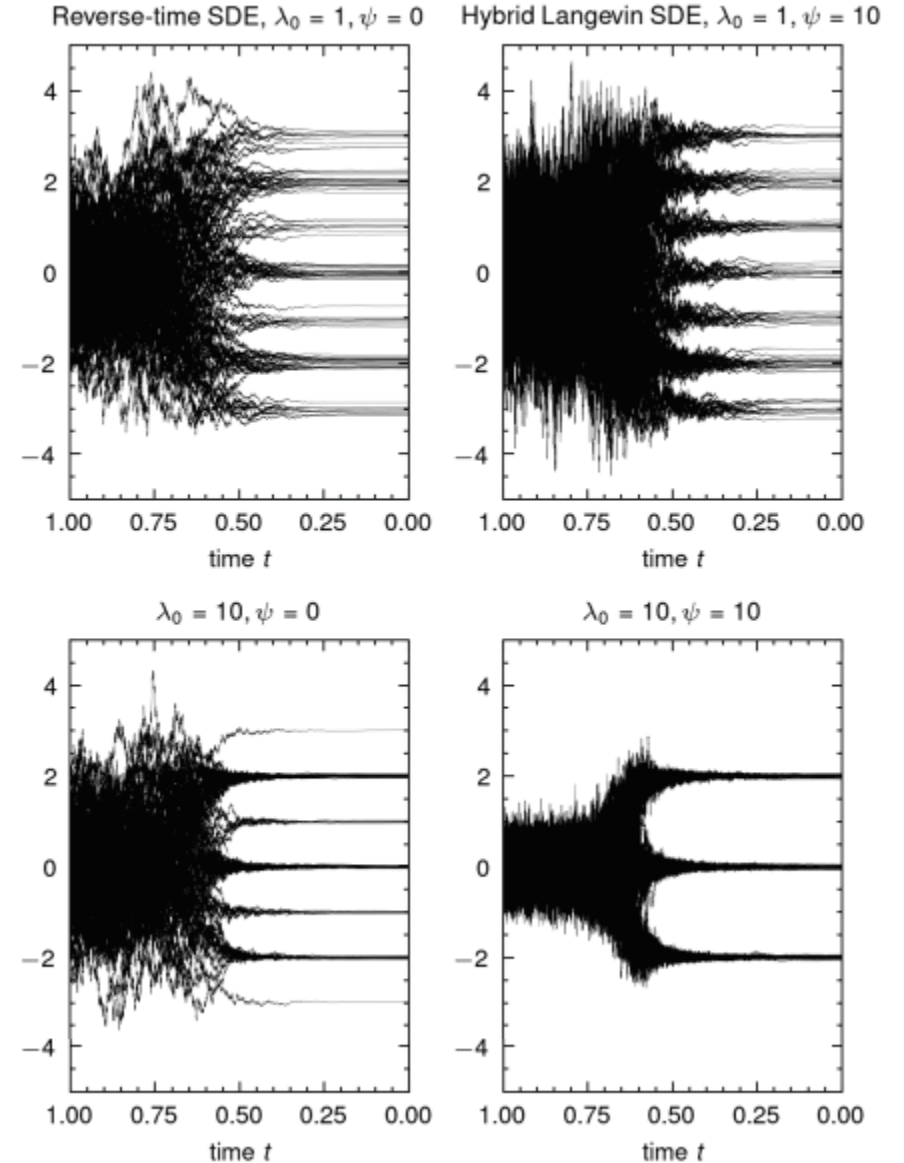


Annealed Langevin dynamics

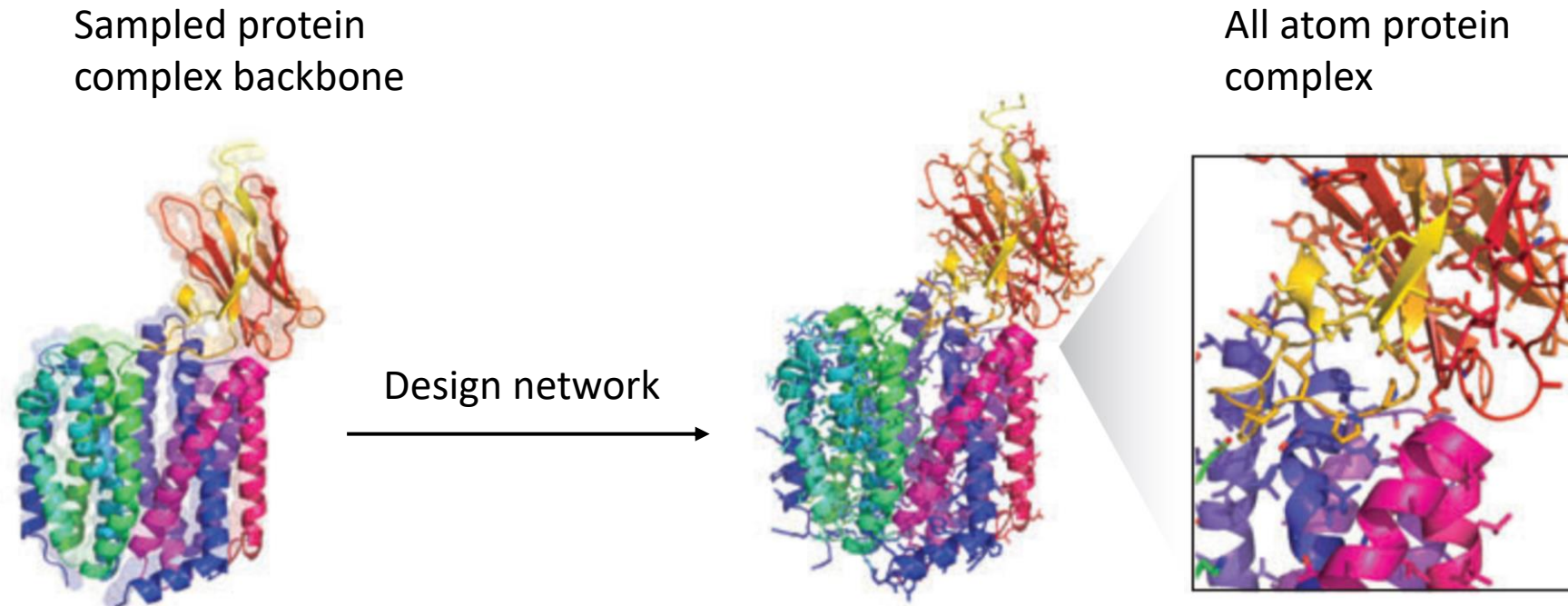


Hybrid Langevin SDE

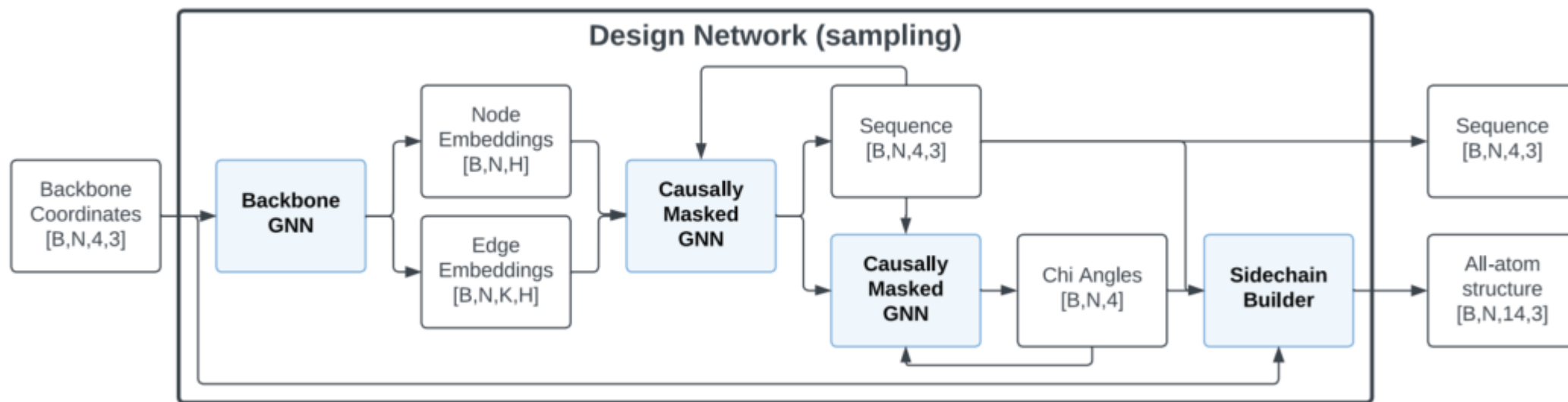
$$dx = \left(-\frac{1}{2}x - \left(\lambda_t + \frac{\lambda_0 \psi}{2} \right) \frac{\sqrt{\alpha_t} \widehat{x}_\theta(x, t) - x}{1 - \alpha_t} \right) \beta_t dt + \sqrt{\beta_t(1 + \psi)} \mathbf{R} d\bar{w}$$



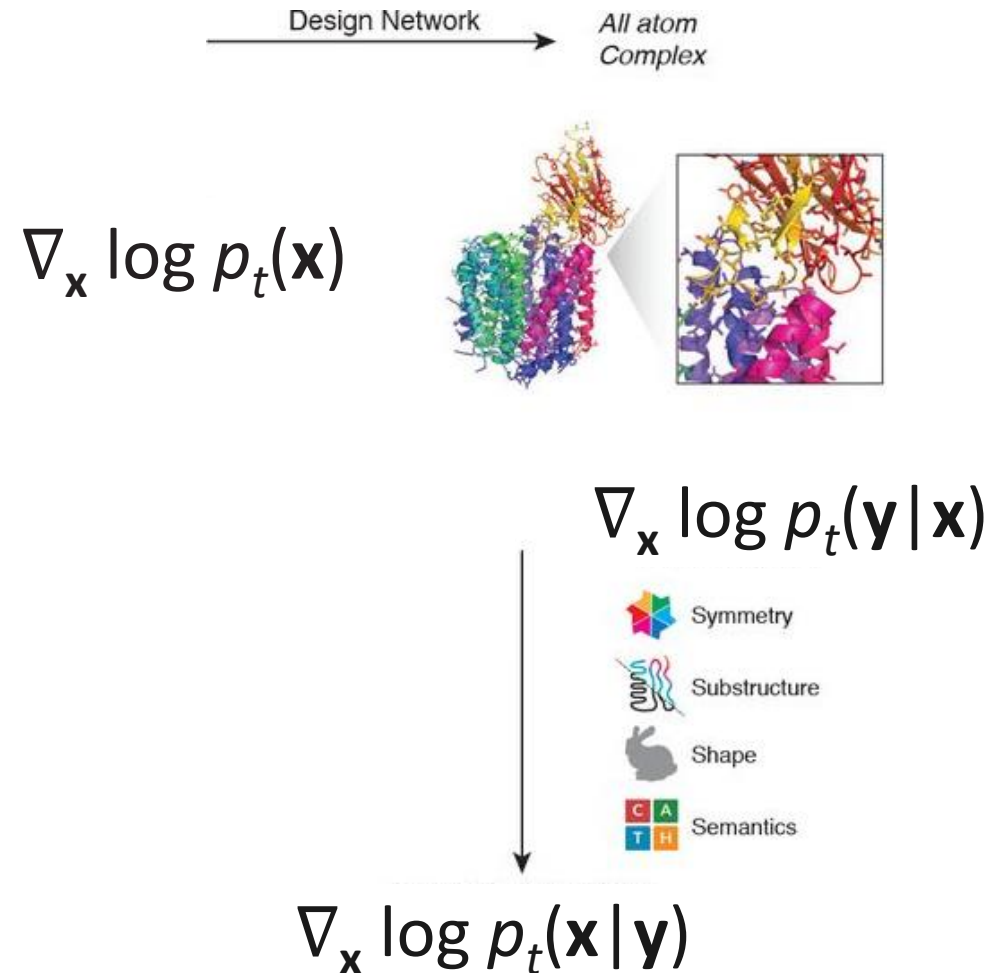
From backbone to sequence and heavy atom position



Design Network



Conditional modeling



Conditional modeling

Bayes' rule

$$p(x|y) = \frac{p(x)p(y|x)}{p(y)}$$

Bayes' rule for score functions

$$\boxed{\nabla x \log p(x)} + \boxed{\nabla x \log p(y|x)} - \cancel{\nabla x \log p(y)}$$

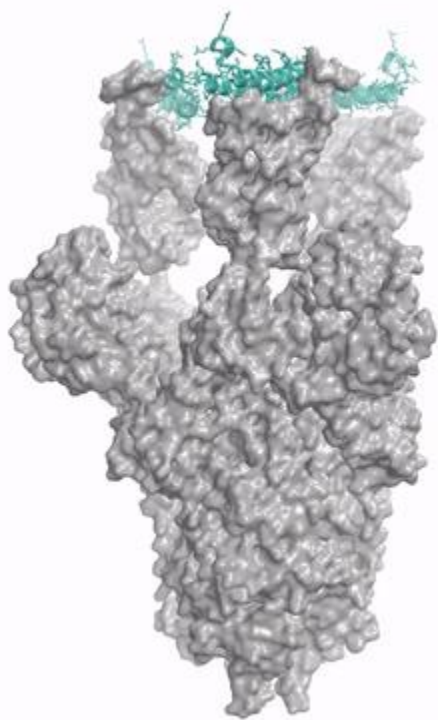
Unconditional
score



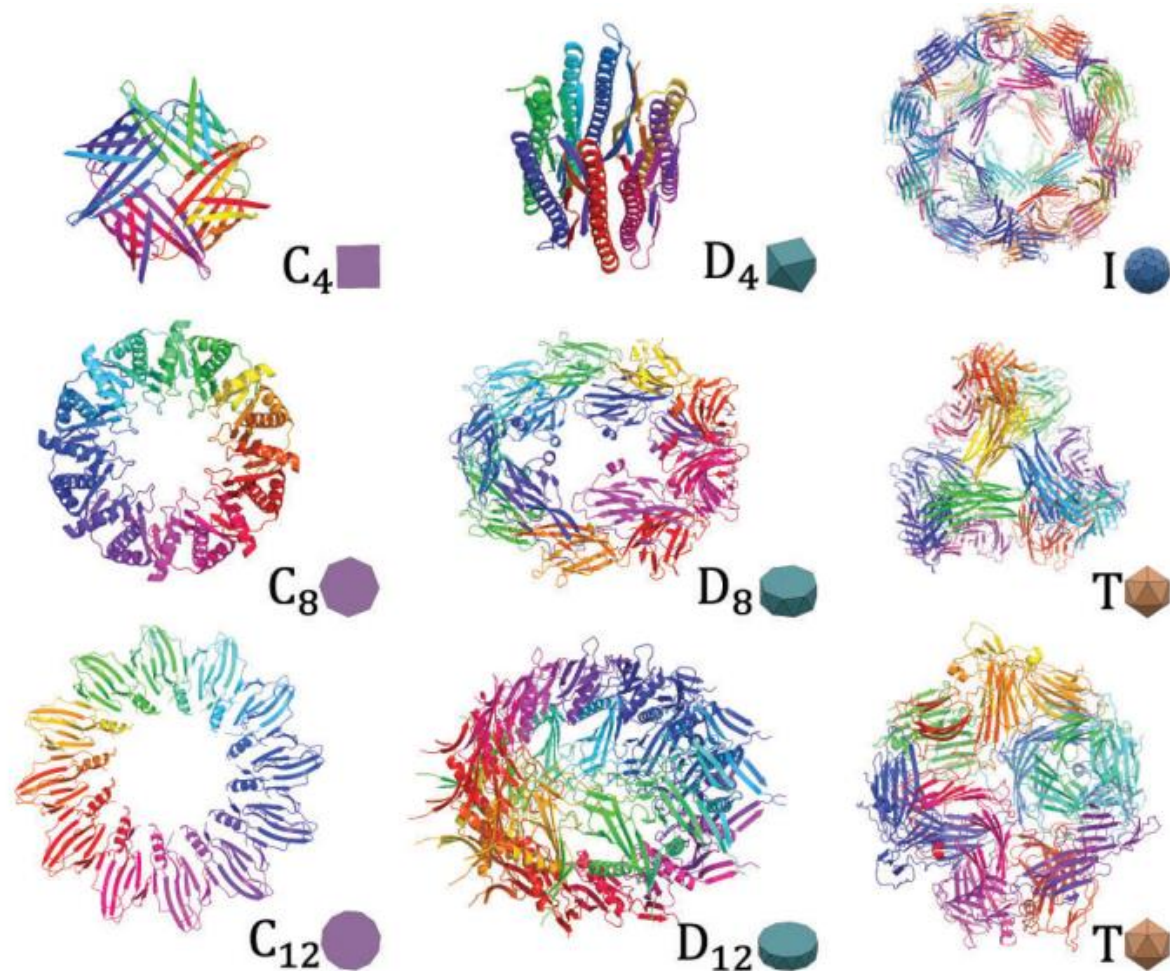
e.g. classifier



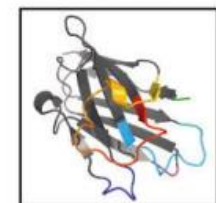
Conditional modeling



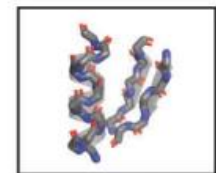
Symmetry and substructure guided diffusion



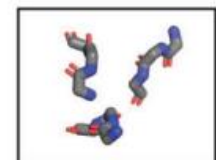
Human DHFR



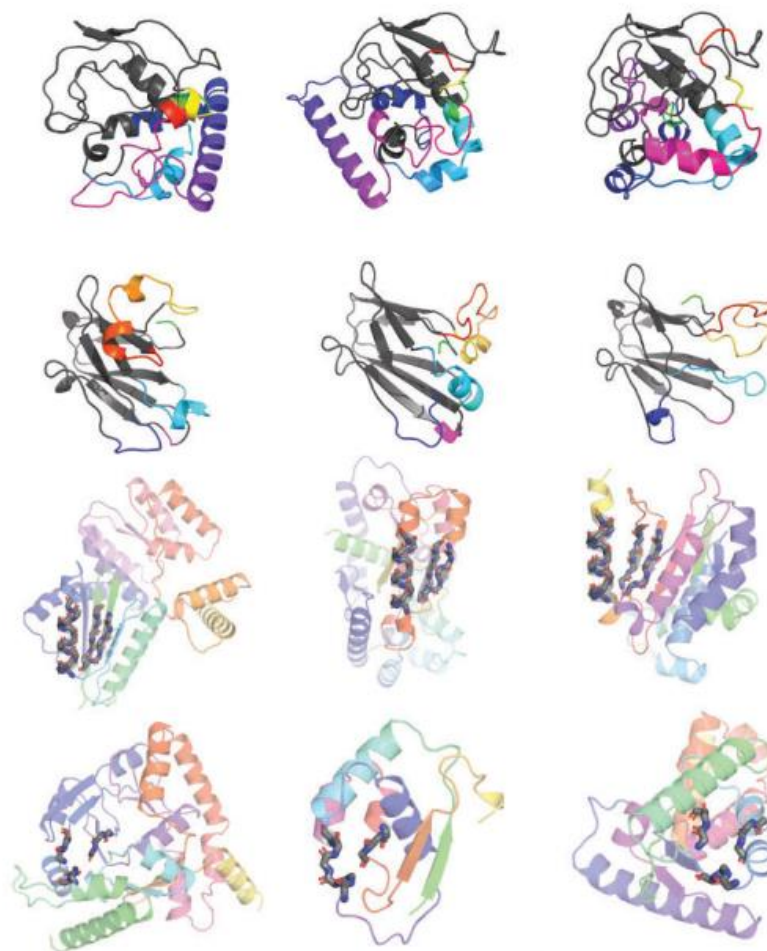
VHH Antibody



$\alpha\beta$ motif



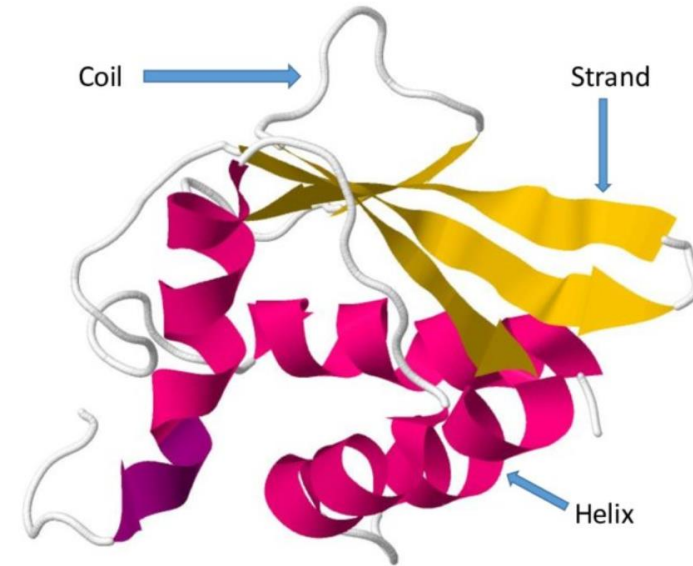
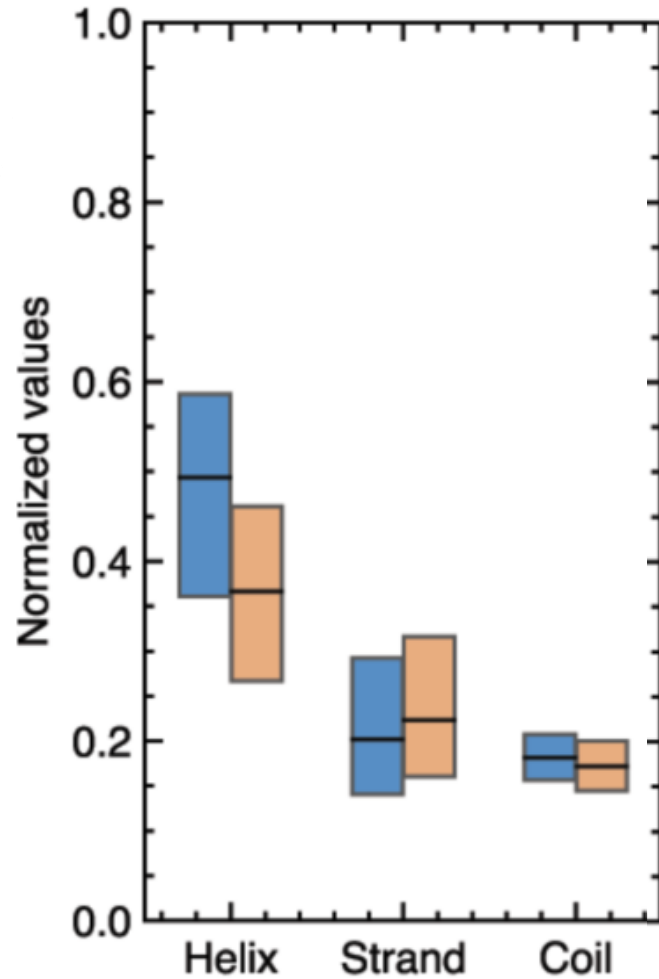
Chymotrypsin triad backbone



Evaluation

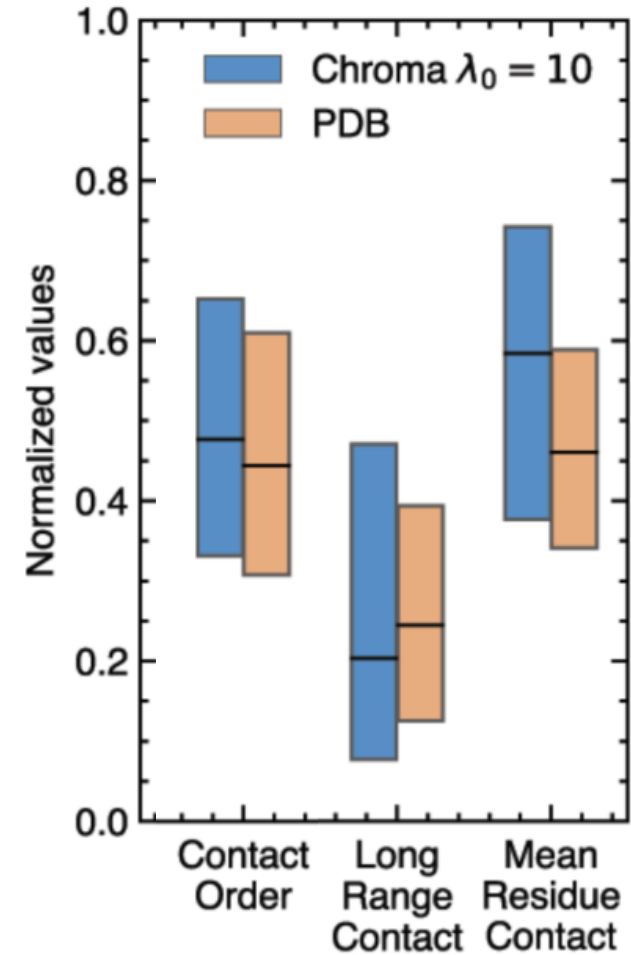
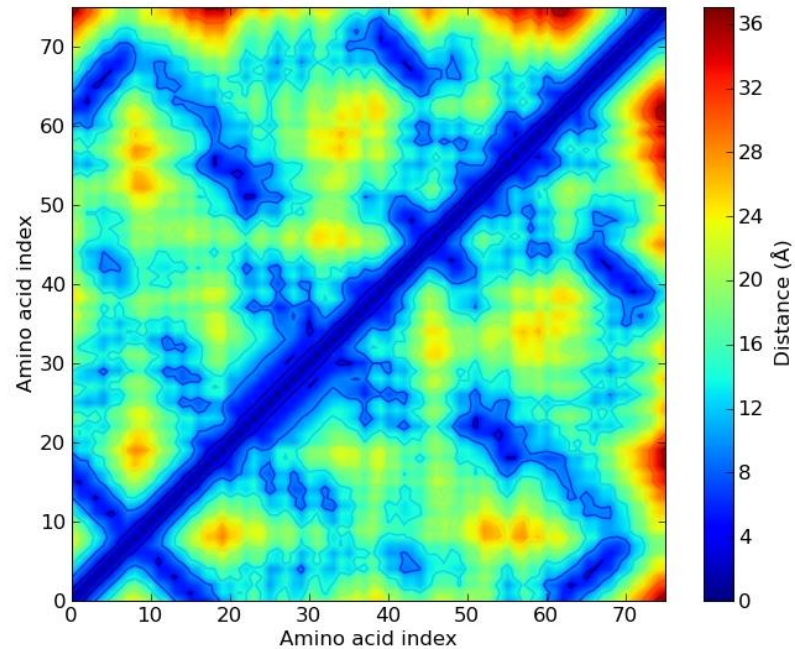
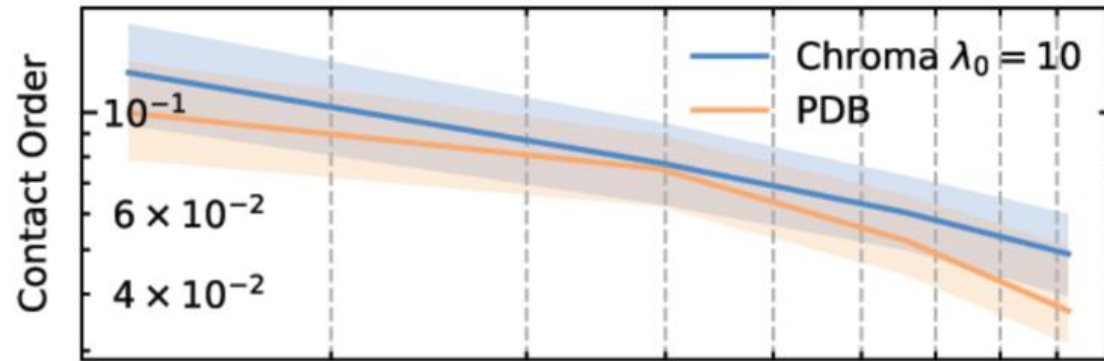
- 50,000 single chains, 10,000 complexes - qualitative
- 10,000 single chain proteins - quantitative
- $\lambda_0 = 10$
- $\psi = 2$
- 200 steps
- Single chain lengths N : $p(N) = 1/N$
- Complex # chain and $N = \#$ chain and N of random complex from PDB

Evaluation – Secondary structures

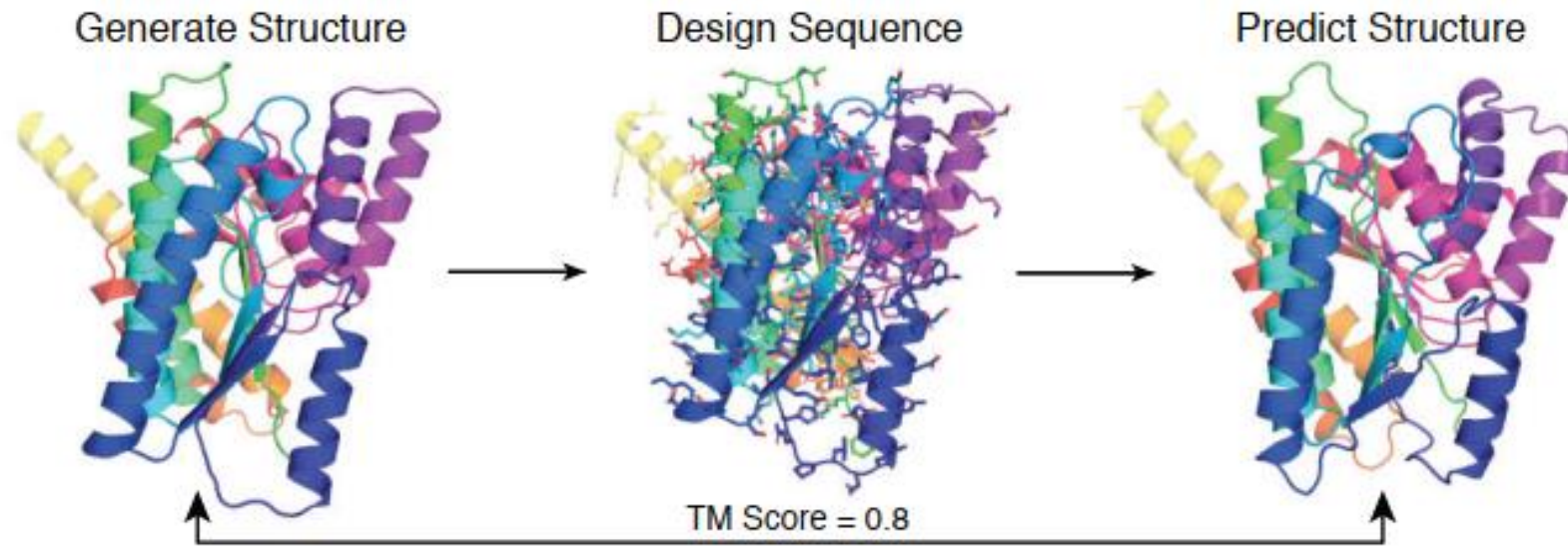


■ Chroma $\lambda_0 = 10$
■ PDB

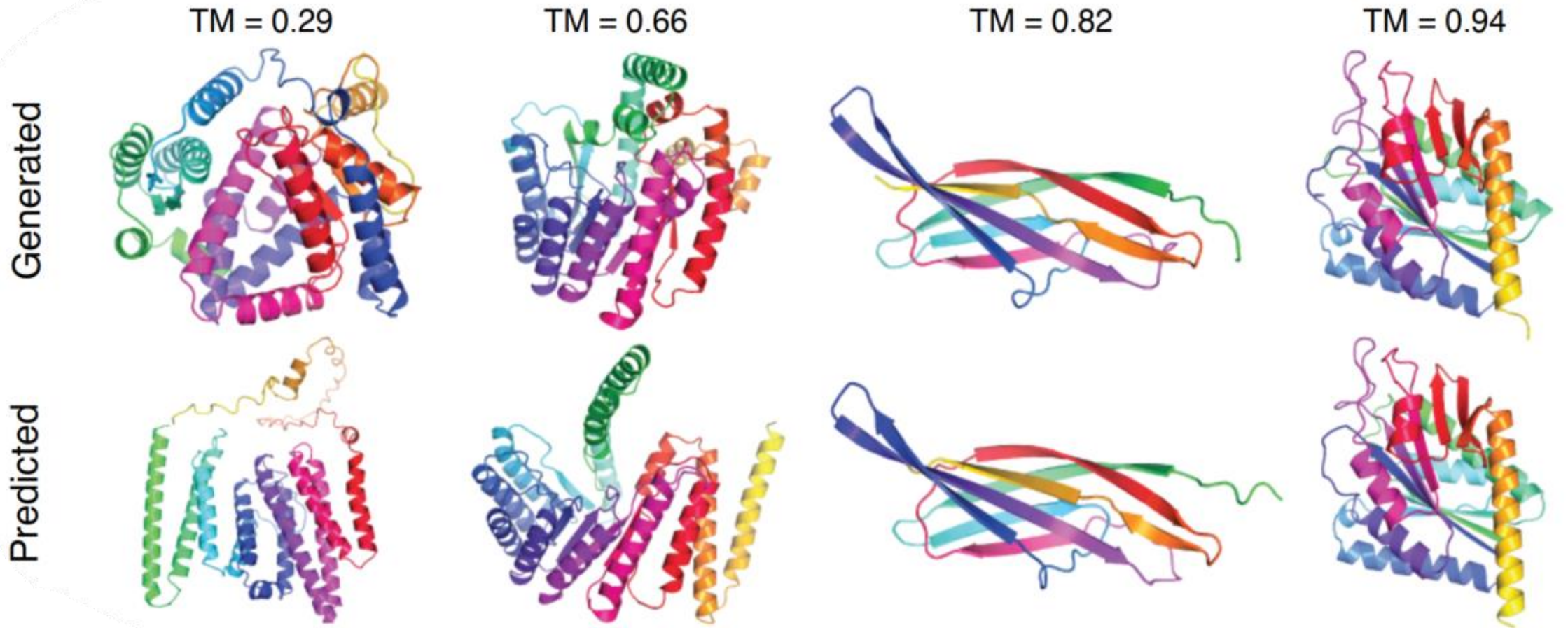
Evaluation – Residue interactions



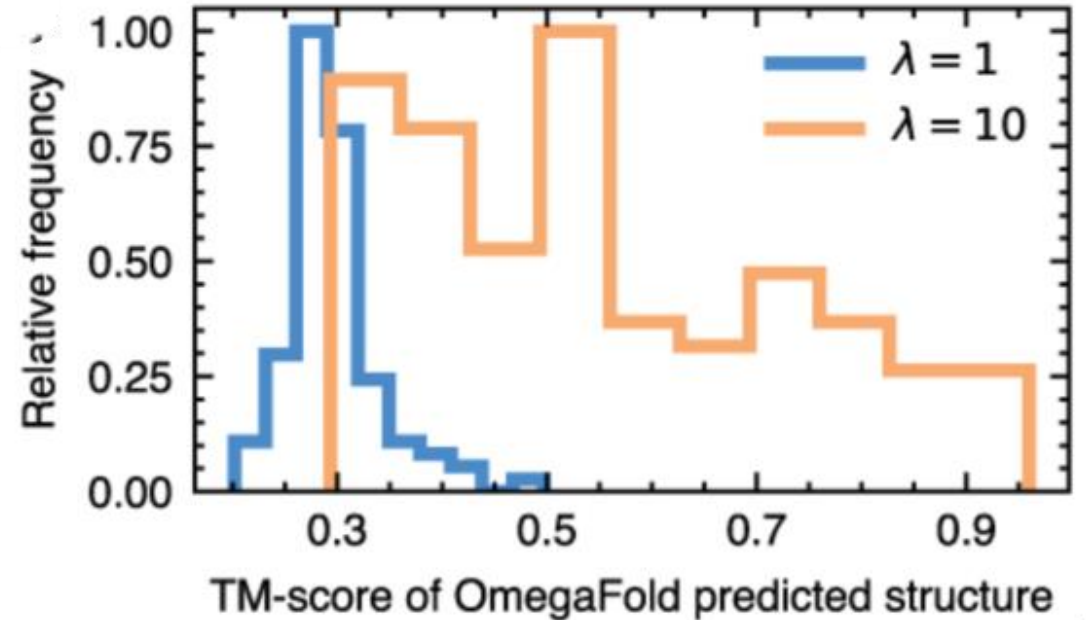
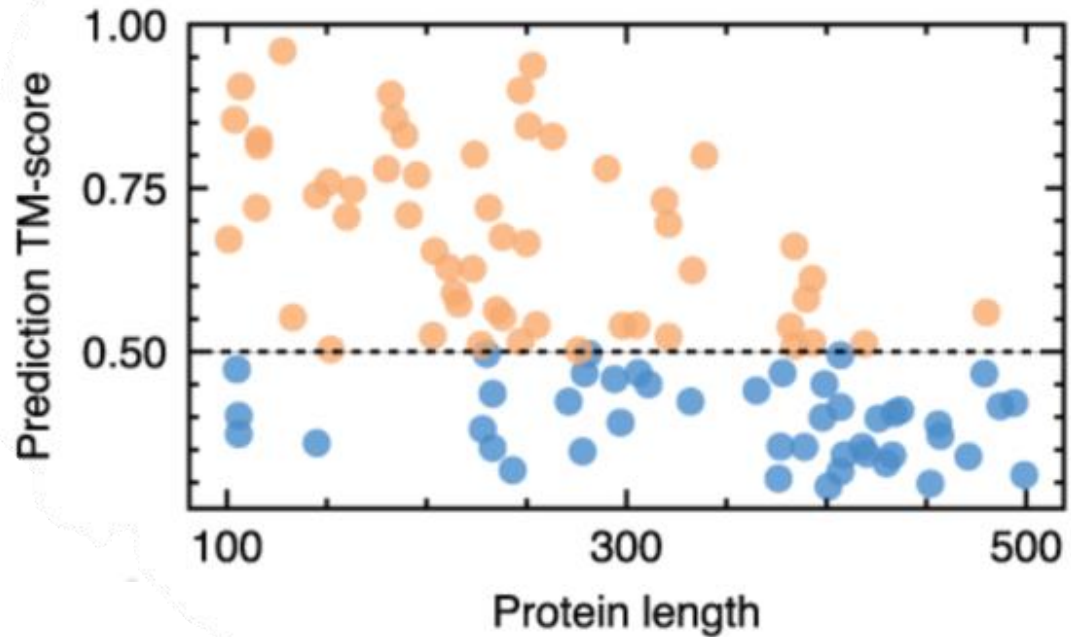
Evaluating Chroma by structure prediction with OmegaFold



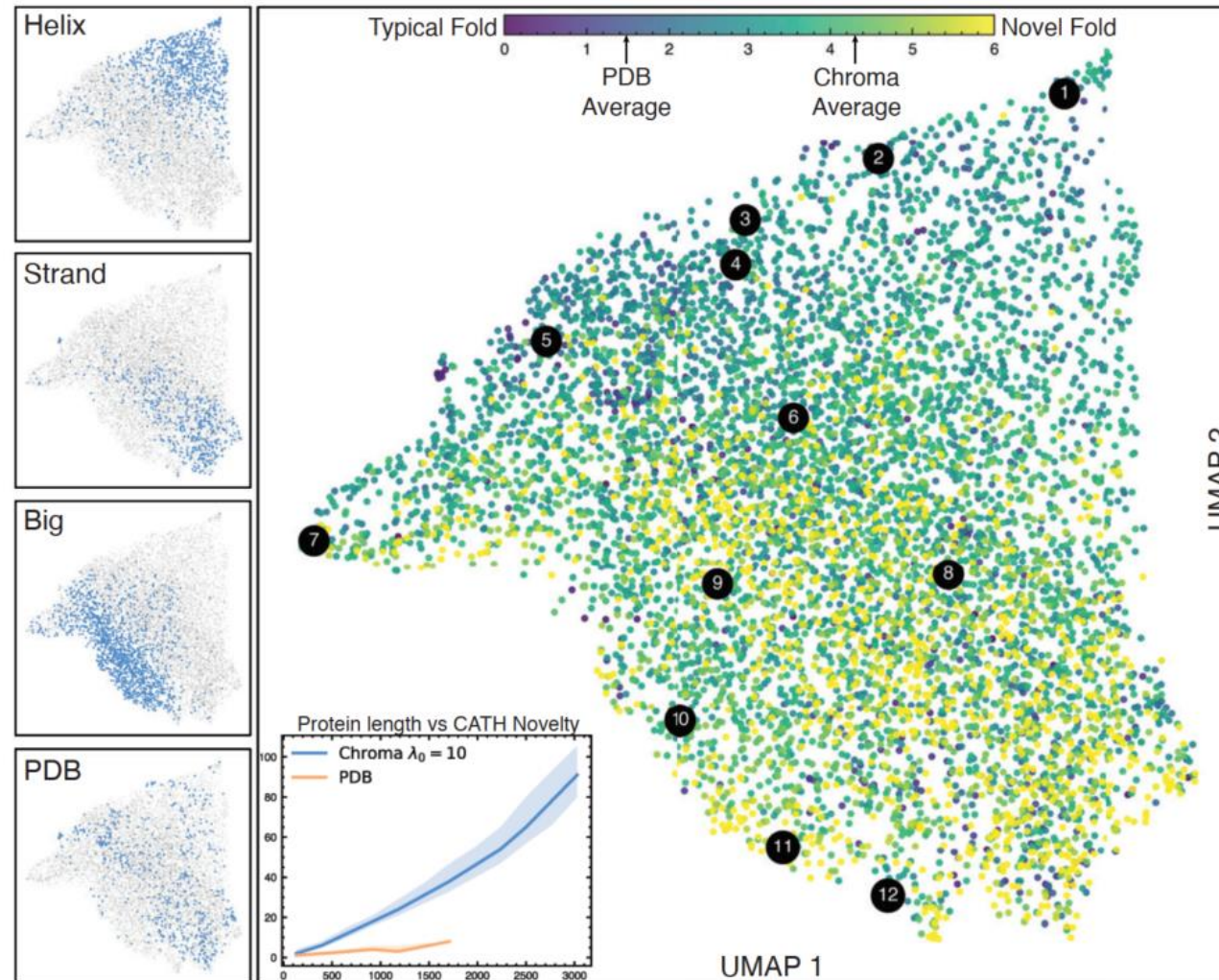
Evaluation - TM-scores



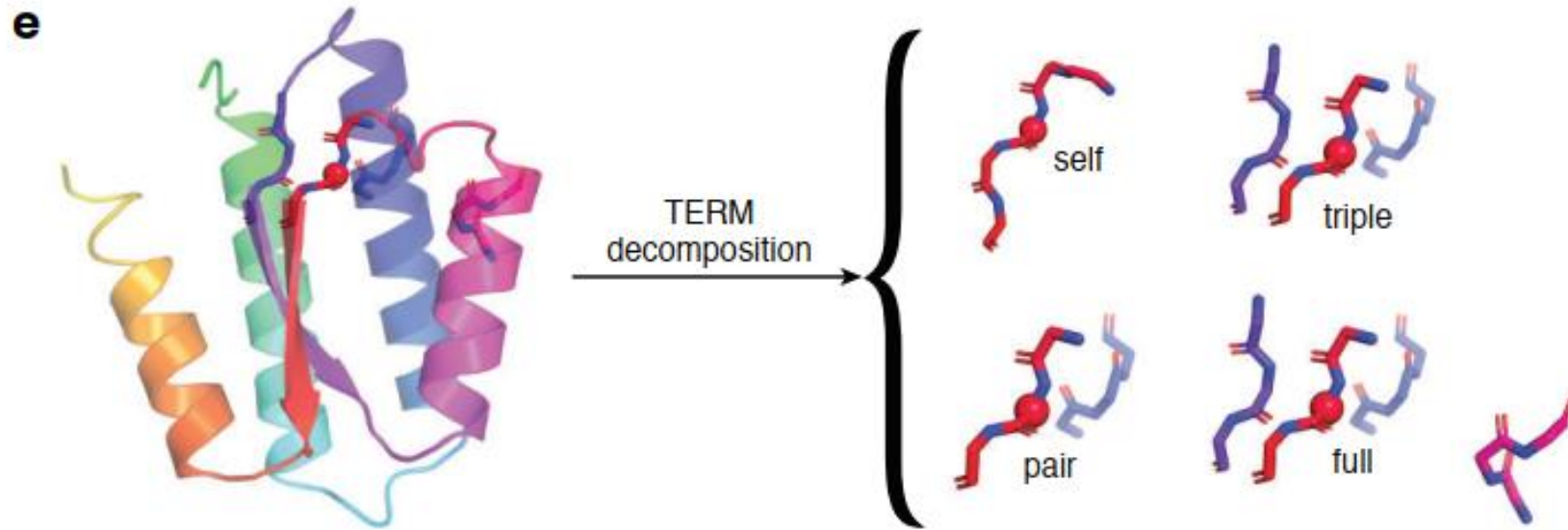
Evaluation - TM-scores



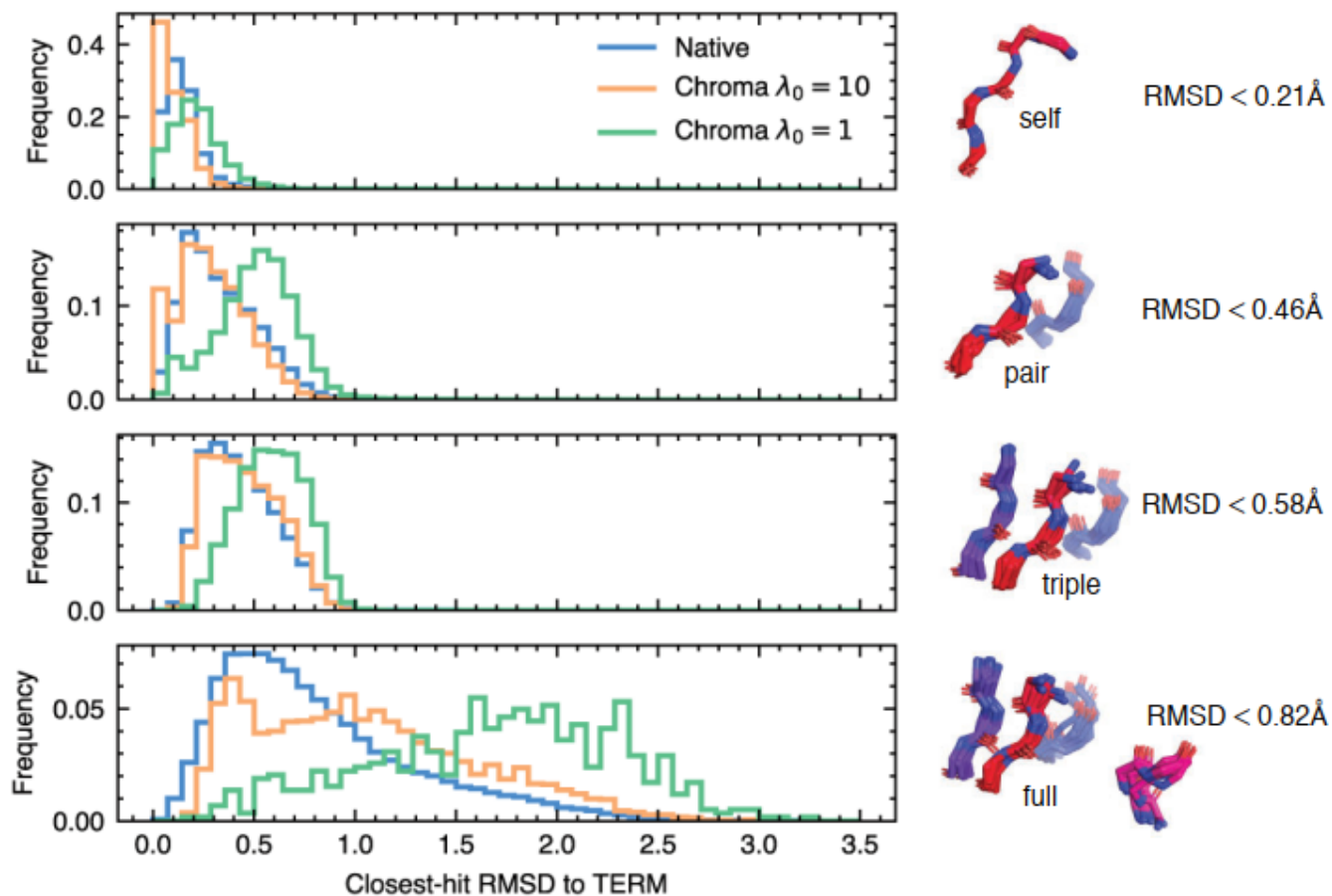
Evaluation - Novelty and structural homology



Evaluation - TERMS



Evaluation - Closest-match RMSD for TERMS



Limitations

- + combination of promising maturities in GDMs
- + elegant way they implement empirical knowledge
- missing experimental characterization
- no quantitative evaluations for many designs and design choices
- no benchmarking
- sequential generation of backbone, sequence and rotamers
- choice of model to evaluate folding

Illuminating chroma?!

